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2023

# The International Mathematical Modeling Challenge (IM<sup>2</sup>C) Summary Sheet To Build or Not To Build: Determining a Quantitative Metric for Land Planning and Allocation

### Summary

Land planning is crucial to ensure that urban development occurs with consideration to the economic, social, and environmental interests of a community. To adhere to optimal land planning, many conflicting factors must often be considered. In this paper, our team makes a quantitative decision metric that can analyze these factors and determine the "best" choice from a given set of development options, as well as the allocation of those choices.

First, **linear programming** is used to determine two "best" development options: one that maximizes both economic and social factors, and one that minimizes negative environmental factors while maximizing social. The maxima and minima from linear programming are then applied to the **Technique for Order of Preference by Similarity to Ideal Solution** to obtain a third real-world "overall best" option that balances economic and environmental factors with a desired weighting. **Genetic algorithm** is then used to determine the optimal positioning of the three established "bests" via an analysis of opportunity costs based off of an environmental degradation penalty index. Finally, the **Cobb-Douglas Function** is used to conduct a short- and long-term analysis of each result's profit by solving **differential equations** with regard to inflation.

This model is then applied to the parcel of land in Victory, NY, using data obtained from research. The ideal option and positioning is found to be **267 acres of sports complex** in the northern half of the land, **129 acres of regenerative farm** directly west of the sports complex, **344 acres of solar array** in the southernmost region of the land, and **1 acre of agritourist centre** on the eastern side of the land.

Conducting a sensitivity analysis on our model reveals that the linear programming results are most affected by the area and societal benefit restrictions, but that the TOPSIS results remain relatively stable regardless of the changing of parameters.

Our model is then adjusted to account for Micron Technology, Inc. building a fabrication facility nearby. As this facility brings more jobs and thus more people, the profit of facilities that involve tourism will increase. However, due to pollution caused by the facility, nature-based facilities will suffer detriments. With these adjustments, the model is re-run, and the results are compared to the previous results. In this scenario, there would be a **greater area of the solar array and agritourist centre**, a **smaller sports complex**, **no regenerative farm**, and **128 acres of ranch**.

Finally, the generalizability of our model is discussed by first discussing its application in Shenzhen, China, and then widening the scope to any location in any country. We conclude that our model will provide the most implementable results in rural environments due to its quantitative nature that cannot consider complicated urban planning laws, but that the model can be applied to nearly any scenario as long as data is provided.

# Keywords: Linear Programming, TOPSIS, Genetic Algorithm, Cobb-Douglas Function, Differential Equation

# LETTER TO DECISION MAKERS

April 2023 | New York, USA

Dear Decision Makers,

Our team has now arrived at a recommendation for the best use of the land in Victory, NY, obtained through a quantitative mathematical model. The model is extremely comprehensive and arrived at its conclusion after a thorough consideration of profit, environmental degradation, carbon emissions, employment, attraction of tourism, recreational offers, and societal benefits.

From our summary sheet, you are likely already aware of our recommended distribution for the land. The image to the right hopefully provides further clarity on that recommendation.





This recommended distribution balances environmental and economic factors in a 1-to-2 ratio. If you were to follow our model's recommendations exactly, your annual profit would be \$9,047,920 USD and the annual CO2 emissions of the finished land developments would be -1,095 tons. Yearby-year profit analysis, including best- and worst-case scenario analyses according to inflation and efficiency, are shown on the graph above. As can be seen, this recommendation can be trusted economically; even the worst-case scenario returns millions in profit by 50 years, and in a best-case scenario, you will be able to make over 250 million in profit at the 50-year mark.

It is worth noting that both the solar array and agritourist center appeared multiple times in our model's recommendation. This did not change whether the model was told to prioritize environmental factors or economic factors, and the pattern remained even when Micron Tech's fab was taken into consideration. Because of this, we highly recommend building at least a **solar array and agritourist center** on the land according to the recommendations.

This summarizes the most pertinent conclusions of our team and our model. Whatever your final decision is regarding this land, we hope you will be able to make an easier decision knowing what the numbers say.

Thank you for your trust in us.

Sincerely,

#### Team 2023001

#### Team #2023001

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2       Total Containing       1         21       Variable Ordinations       1         22       Assumptions in Jernmons       2         3       Instri Research       2         3.3       Linear Programming for Preliminary Planning       4         3.4       TotPSIS for Working Model       5         3.4       TotPSIS for Working Model       5         3.5       Cenetric Algorithm       6         3.5       Prediction       6         3.6       Short- and Long-term Considerations       8         4       TotR Store Considerations       8         4       TotR Store Considerations       9         4.1       Data Considerations       10         4.2       TotR Store Considerations       10         4.2       Th	•		1
3     Task 1: Ceasing the Model     2       11     Initial Reserve     2       12     Citeria Identification     3       13     Linear Programming for Poliminary Planning     4       14     TOPES for Westing Model     4       15     Total Reserve     4       16     Total Reserve     4       17     Criteria Identification     4       18     Total Reserve     4       19     Total Reserve     5       10     Total Reserve     5       11     Introduction to TOPESIS     5       12     Criteria Identification     6       13.1     Forces or Correct Application     6       13.2     Application of Correctic Algorithm     8       13.6     Totak 2: Application of Correctic Algorithm     8       14     Date Collection     10       12     Totak 2: Application and Sensitivity Analysis     9       14     Date Collection     10       12     Totak 2: Application and Sensitivity Analysis     10       14     Date Collection     10       12     Totak 2: Reservaluation     10       12     Totak 2: Reservaluation     11       14     2: Sensitrity Analysis of TOPSIS     14       <	2	Preliminary Assumptions and Definitions         2.1       Variable Definitions         2.2       Assumptions	1 . 1 . 2
3       Justic Toreaning interModel       2         3       Initial Seconds       2         3       Linear Programming for Preliminary Planning       4         3.3       Linear Programming for Preliminary Planning       4         3.3       Invitormental       4         3.3       Torestion Working Model       5         3.4       TORES for Working Model       5         3.5       Genetic Algorithm (GA) for Application       6         3.5       Torest of Working Model       5         3.5       Torest of Working Model       5         3.5       Torest of Working Model       6         3.5       Torest of Considerations       6         3.5       Torest of Considerations       8         4       Task 2: Application of Considerations       9         4.1       Task 2: Application and Sensitivity Analysis       9         4.2       Torest Results       10         4.2.1       There Programming Results       11         4.2.2       Application Accelerations       11         4.2.3       Genetic Algorithm Results       14         4.3       Second Acceleration and Second micests       14         4.3       Second Acceleration and			
3.1       Industry Results       2         3.2       Clinical Resultation       3         3.3       Linear Programming for Philmmary Planning       4         3.4       Linear Encommental       4         3.4       Linear Encommental       4         3.4       Linear Encommental       4         3.4       Linear Encommental       5         3.4.1       Linear Encommental       6         3.5       Cenetic Algorithm (ColS)S       5         3.4.2       LONES for Working Model       5         3.5       Cenetic Algorithm       6         3.5       Cenetic Algorithm       6         3.6       Shut-mall Congetern Curside Algorithm       8         3.6       Shut-mall Congetern Curside Algorithm       8         3.6       Shut-mall Congetern Curside Algorithm       9         4.1       Data Collection       10         4.2.1       Innear Programming Results       10         4.2.2       COSES Results       11         4.2.3       Sensitivity Analysis of Linear Programming       14         4.3.4       Sensitivity Analysis of Linear Programming       14         4.3.5       Senstivity Analysis of Linear Programming       14	3	Task 1: Creating the Model	2
2-2       Cincil Indentify Sign Philimstry Planning       4         3.3       Linear Programming for Philmstry Planning       4         3.3.1       Foruromic       4         3.3.2       Foruromic       4         3.3.4       TOPSIS for Working Model       5         3.4.1       Initiadization to TOPSIS       5         3.4.2       TOPSIS in Our Model       5         3.5       Genetic Algorithm (CA) for Application       6         3.5.1       Process of Genetic Algorithm       6         3.5.3       Short- and Lang-term Cursiderations       8         4       Table 2. Application of Genetic Algorithm       6         3.5.2       Application of Genetic Algorithm Results       10         4.1       Data Collection       10         4.2       The "Best" Option       10         4.2.1       Linear Programming Results       11         4.2.2       Short and Lang-tern Results       11         4.2.3       Genetic Algorithm Results       12 </td <td></td> <td>3.1 Initial Research</td> <td>. 2</td>		3.1 Initial Research	. 2
33.1       Execution       4         33.2       Environmental       4         34       TUSES in Curk Model       5         34.1       Introduction to TOPSIS       5         34.2       TOUSES in Qurk Model       5         35.3       Caretic: Algorithm       6         35.3       Caretic: Algorithm       6         35.3       Caretic: Algorithm       6         35.4       Application and Sensitivity Analysis       9         4       Date Collection       10         4.2.1       Incore Togramming Results       10         4.2.2       TOPSIS Kouths       10         4.2.1       Incore Togramming Results       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Sensitivity Analysis       14         4.3.5       Sensitivity Analysis of TOPSIS       14         4.3.1       Sensitivity Analysis of TOPSIS       14         4.3.2       Sensitivity Analysis of TOPSIS       15         5       Ast Coregin Enclipt Profit       17         5.1.1       Change in Restrictons       17         5.1.2       Change in Restrictons       17         5.1.4       Change in Rest		3.3 Linear Programming for Preliminary Planning	. 5
3.3.2       Environmental       4         3.4       Introduction to TOPSIS       5         3.4.1       Introduction to TOPSIS       5         3.4.2       TOPSIS in Our Model       5         3.5       Center Algorithm (CA) for Application       6         3.5.1       Process of Genetic Algorithm       6         3.5.2       Application of Genetic Algorithm       8         3.6       Shurt- and Long-term Considerations       8         4       Task 2: Application and Sensitivity Analysis       9         4.1       Data Collection       10         4.2       The "Rest" Option       10         4.2.1       Incore Trogramming Results       11         4.2.2       Conctic Algorithm Results       11         4.2.3       Sensitivity Analysis       14         4.3       Sensitivity Analysis       14         4.3.3       Sensitivity Analysis       14         4.3.4       Sensitivity Analysis       14         4.3.5       Sensitivity Analysis       14         4.3.1       Sensitivity Analysis       14         4.3.2       Sensitivity Analysis       14         4.3.3       Sensitivity Analysis       14		3.3.1 Economic	. 4
3.4       TOPSIS for Working Model       5         3.4.1       Introduction to TOPSIS       5         3.5.2       Credit Algorithm (GA) for Application       6         3.5.1       Process of Cenetic Algorithm       6         3.5.2       Application of Cenetic Algorithm       6         3.5.3       Fonces of Cenetic Algorithm       6         3.5.4       TopPlication of Cenetic Algorithm       6         3.6       Short- and Long-term Considerations       8         4       Task 2: Application of Cenetic Algorithm       6         4.2       The "Best" Option       00         4.2.1       Linear Programming Results       00         4.2.2       TOPIS'B Results       11         4.2.3       Sensitivity Analysis of Linear Programming .       14         4.3.1       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech, Inc.       17         5.1       Change in Facility Profit       17         5.1.2       Change in Facility Profit       17         5.1		3.3.2 Environmental	. 4
34.1       Introduction to TOPSIS       5         34.2       TOPSIS in Our Model       5         35.       Genetic Algorithm       6         35.1       Process of Genetic Algorithm       6         35.2       Application of Genetic Algorithm       6         36.       Short- and Long-term Considerations       8         4       Task 2: Application and Sensitivity Analysis       9         4.1       Data Collection       10         4.2.1       Linear Programming Results       10         4.2.2       ToPSIS (or dubin of Sensitivity Analysis       10         4.2.2       TOPSIS exults       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Sensitivity Analysis of Tinner Programming       14         4.3       Sensitivity Analysis of TIOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1.1       Change in Results       17         5.1.2       Change in Results       17         5.1.2       Change in Results       17         5.1.4       Change in Results       17         5.1.7       Sensitivity Analysis of TIOPSIS       16         6       Task 4: Corec		3.4 TOPSIS for Working Model	. 5
3.42       TOPSIS in Our Model       5         3.5       Genetic Algorithm (CA) for Application       6         3.5.1       Process of Center, Algorithm       6         3.5.2       Application of Genetic Algorithm       8         3.6       Bott- and Long-term Considerations       8         4       Task 2: Application and Sensitivity Analysis       9         4       Ibat Collection       10         4.2       The "Best" Option       10         4.2.1       Innex Programming Results       10         4.2.2       TopSits Results       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Sonsitivity Analysis       14         4.3       Sonsitivity Analysis       14         4.3       Sonsitivity Analysis       14         4.3       Sonsitivity Analysis       16         5       Task 3: Re-evaluation for Micron Tech, Inc.       17         5.1       Affected Factors       17         5.1       Conclusion and Evaluation       17         5.1       Change in Facility Profit       17         5.1       Change in Facility Profit       17         5.1       Conclusion and Evaluation       16		3.4.1 Introduction to TOPSIS	. 5
3.5       Genetic Algorithm (GA) for Application       6         3.5.1       Process of Genetic Algorithm       6         3.5.2       Application of Genetic Algorithm       8         3.6       Shurt- and Long-term Considerations       8         4       Task 2: Application and Sensitivity Analysis       9         4.1       Data Collection       10         4.2       The "Best" Option       10         4.2       Linear Programming Results       10         4.2.1       Linear Programming Results       10         4.2.2       OPINI mesults       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Short- and Long-term Results       14         4.3       Sensitivity Analysis of Linear Programming       14         4.3       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Alfected Factors       17         5.1.4       Change in Restrictions       17         5.1.2       New Plan       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       20         7       Conclusion and Evaluati		3.4.2 TOPSIS in Our Model	. 5
3.5.1       Process of Genetic Algorithm       6         3.5.2       Application of Genetic Algorithm       8         3.6       Short-and Long-term Considerations       8         4       Task 2: Application and Sensitivity Analysis       9         4.1       Data Collection       10         4.2       The "Best" Option       10         4.2.1       The "Best" Option       10         4.2.1       Inter Programming Results       10         4.2.2       TOPSIS Results       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Stort- and Long-term Results       12         4.3       Sensitivity Analysis of Linear Programming       14         4.3       Sensitivity Analysis of TOPSIS       16         5       Task 3: Resvaluation for Micron Tech., Inc.       17         5.1       Affected Tactors       17         5.1.1       Change in Restrictores       17         5.1.2       Change in Restrictores       17         5.1       Affected Tactors       17         5.1.2       Conclusion and Evaluation       19         6.1       Familiar Contoxts       20         7       Conclusion and Evaluation		3.5 Genetic Algorithm (GA) for Application	. 6
3.52       Application of Genetic Algorithm       8         3.6       Short- and Long-term Consideration       8         4       Task 2: Application and Sensitivity Analysis       9         4.1       Data Cellection       10         4.2       The "Best" Option       10         4.2.1       Linear Programming Results       10         4.2.2       TOPSIS Results       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Short- and Long-term Results       11         4.2.5       Sensitivity Analysis       14         4.3       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1.1       Change in Rectitity Pofit       17         5.1.2       Change in Rectintens       10         <		3.5.1 Process of Genetic Algorithm	. 6
3.6       Short- and Long-term Considerations       8         4       Task 2: Application and Sensitivity Analysis       9         4.1       Data Collection       10         4.2       The "Best" Option       10         4.2       The "Best" Option       10         4.2.1       Linear Programming Results       10         4.2.2       TOPSIS Results       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Softwitz Analysis of Linear Programming       14         4.3       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of ToPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Alfeeded Factors       17         5.1.1       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.1.4       Genetic Algorithm       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7.2       Conclusion <td></td> <td>3.5.2 Application of Genetic Algorithm</td> <td>. 8</td>		3.5.2 Application of Genetic Algorithm	. 8
4       Task 2: Application and Sensitivity Analysis       9         4.1       Data Collection       10         4.2       The "Best" Option       10         4.2.1       Linear Programming Results       10         4.2.2       TOTSIS Results       11         4.2.3       Centic Algorithm Results       11         4.2.4       Short- and Long-item Results       11         4.2.5       Centic Algorithm Results       11         4.2.6       Short- and Long-item Results       14         4.3       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech, Inc.       17         5.1       Alfeender Factors       17         5.1.2       Change in Facility Profit       17         5.1.2       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.1.2       Change in Restrictions       19         6       Task 4: Ceneralizability       18         6.1       Familiar Contexts       19         7.2       Conclusion and Evaluation       20         7.1       Loulaution of Strengths and Data       22         Appendix B       All learning Curves and Final DNA of		3.6 Short- and Long-term Considerations	. 8
4.1       Data Collection       10         4.2       The "Best" Option       10         4.2.1       Linear Programming Results       10         4.2.2       Genetic Algorithm Results       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Short- and Long-term Results       14         4.3       Sensitivity Analysis       14         4.3.3       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Change in Facility Profit       17         5.1.1       Change in Facility Profit       17         5.1.2       Change in Restrictions       17         5.2       New Plan       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7       Conclusion       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.1       Evaluation of Strengths and Data       22 <t< td=""><td>4</td><td>Task 2: Application and Sensitivity Analysis</td><td>9</td></t<>	4	Task 2: Application and Sensitivity Analysis	9
4.2       The "Best" Option       10         4.2.1       Linear Programming Results       10         4.2.2       TOFSIS Results       11         4.2.3       Cencic Algorithm Results       11         4.2.4       Short- and Long-term Results       11         4.2.4       Short- and Long-term Results       14         4.3       Sensitivity Analysis of Linear Programming       14         4.3       Sensitivity Analysis of IOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Affected Factors       17         5.1.2       Change in Facility Profit       17         5.1.2       Change in Restrictions       17         5.2       New Plan       18         6.1       Familiar Contexts       19         6.2       Lond in Other Countries       20         7       Conclusion and Evaluation       20         7.1       Evaluation       21         7.2       Conclusion       21         Appendix A       Substantiating Tables and Data       22         Appendix B       All learning Curves and Final DNA of Genetic Algorithm       23         Appendix C       Genetic Algorithm DNA Graph Code		4.1 Data Collection	. 10
4.2.1Linear Programming Results104.2.2TOPSIS Results114.2.3Genetic Algorithm Costlis114.2.4Short- and Long-term Results144.3Sensitivity Analysis144.3Sensitivity Analysis of Linear Programming144.3.1Sensitivity Analysis of Linear Programming144.3.2Sensitivity Analysis of Inicar Programming144.3.3Sensitivity Analysis of Inicar Programming144.3.4Sensitivity Analysis of TOPSIS165Task 3: Re-evaluation for Micron Tech, Inc.175.1Affected Factors175.1.2Change in Facility Profit175.1.2Change in Restrictions175.1.2Change in Restrictions175.2New Plan186.1Factility186.1Familiar Contexts207Conclusion and Evaluation207.1Facturation207.2Conclusion and Evaluation207.2Conclusion of Strengths and Weaknesses207.2Conclusion and Evaluation207.4Appendix ASubstantiating Tables and Data22Appendix BAll learning Curves and Final DNA of Genetic Algorithm23Appendix CGenetic Algorithm Code31Appendix ELinear Programming Code31Appendix FTOPSIS Code34		4.2 The "Best" Option	. 10
4.2.2       TOPSIS Results       11         4.2.3       Genetic Algorithm Results       11         4.2.4       Short- and Long-term Results       11         4.3       Sensitivity Analysis       14         4.3       Sensitivity Analysis of Linear Programming       14         4.3.1       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Affected Factors       17         5.1.1       Change in Restrictions       17         5.2       New Plan       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7       Conclusion and Evaluation       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.1       Evaluation       20         7.1       Evaluation       20         7.2       Conclusion       20         7.3       Conclusion       20         7.4       Evaluation       20         7.5       Conclusion       20         7.6       Conclusion       20		4.2.1 Linear Programming Results	. 10
42.3       Genetic Algorithm Results       11         4.2.4       Short- and Long-term Results       14         4.3       Sensitivity Analysis of Linear Programming       14         4.3.1       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Affected Factors       17         5.1.1       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.1.3       Change in Restrictions       17         5.1.4       Chenealizability       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7.2       Conclusion and Evaluation       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.4       Evaluation of Strengths and Data       22         Appendix A       Substantiati		4.2.2 TOPSIS Results	. 11
42.4       Short- and Long-term Results       14         4.3       Sensitivity Analysis       14         4.3.1       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech, Inc.       17         5.1       Affected Factors       17         5.1.1       Change in Facility Profit       17         5.1.2       Change in Restrictions       17         5.2       New Plan       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7       Conclusion and Evaluation       20         7.2       Conclusion       20         7.4       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.4       Evaluation and Evaluation       20         7.2       Conclusion       21		4.2.3 Genetic Algorithm Results	. 11
4.3       Sensitivity Analysis       14         4.3.1       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Affected Factors       17         5.1.1       Change in Facility Profit       17         5.1.2       Change in Restrictions       17         5.2       New Plan       18         6.1       Familiar Contexts       19         6.2       Land in Other Contries       20         7       Conclusion and Evaluation       20         7.1       Conclusion       20         7.2       Conclusion       20         7.3       Conclusion       20         7.4       Conclusion       20         7.5       Conclusion       20         7.4       Evaluation       20         7.5       Conclusion       20         7.1       Evaluation       20         7.2       Conclusion       20         7.4       Evaluation       20         7.5       Conclusion       20         8       Allearning Tables and Data <td></td> <td>4.2.4 Short- and Long-term Results</td> <td>. 14</td>		4.2.4 Short- and Long-term Results	. 14
4.3.1       Sensitivity Analysis of Linear Programming       14         4.3.2       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Affected Factors       17         5.1.1       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.2       New Plan       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7       Conclusion and Evaluation       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.4       Conclusion       20         7.5       Conclusion       20         7.1       Evaluation       20         7.2       Conclusion       20         7.3       Conclusion       20         7.4       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         References       21       Appendix A Substantiating Tables and Data       22         Appendix B		4.3 Sensitivity Analysis	. 14
4.3.2       Sensitivity Analysis of TOPSIS       16         5       Task 3: Re-evaluation for Micron Tech., Inc.       17         5.1       Affected Factors       17         5.1.1       Change in Facility Profit       17         5.1.2       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.1.2       Change in Restrictions       17         5.1.2       New Plan       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7       Conclusion and Evaluation       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.4       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.2       Conclusion       20         7.4       Evaluation of Strengths and Data       22         Appendix A       Substantiating Tables and Data       22         Appendix B       All learning Curves and Final DNA of Genetic Algorithm       23         Appendix C       Genetic Algorithm DNA Graph C		4.3.1 Sensitivity Analysis of Linear Programming	. 14
5     Task 3: Re-evaluation for Micron Tech., Inc.     17       5.1     Affected Factors     17       5.1.1     Change in Facility Profit     17       5.1.2     Change in Restrictions     17       5.1.2     Change in Restrictions     17       5.1.2     New Plan     17       5.2     New Plan     18       6.1     Familiar Contexts     19       6.2     Land in Other Countries     20       7     Conclusion and Evaluation     20       7.1     Evaluation of Strengths and Weaknesses     20       7.2     Conclusion     20       7.3     Evaluation of Strengths and Weaknesses     20       7.4     Evaluation of Strengths and Weaknesses     20       7.2     Conclusion     20       7.4     Evaluation of Strengths and Meaknesses     20       7.2     Conclusion     20       7.4     Evaluation of Strengths and Meaknesses     20       7.2     Conclusion     20       7.4     Evaluation of Strengths and Data     22       Appendix A     Substantiating Tables and Data     22       Appendix C     Genetic Algorithm DNA of Genetic Algorithm     23       Appendix C     Genetic Algorithm DNA Graph Code     31       Ap		4.3.2 Senstivity Analysis of TOPSIS	. 16
5.1       Affected Factors       17         5.1.1       Change in Facility Profit       17         5.1.2       Change in Restrictions       17         5.2       New Plan       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7       Conclusion and Evaluation       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.3       Evaluation of Strengths and Weaknesses       20         7.4       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         References       21         Appendix A       Substantiating Tables and Data       22         Appendix B       All learning Curves and Final DNA of Genetic Algorithm       23         Appendix C       Genetic Algorithm DNA Graph Code       31         Appendix D       Genetic Algorithm DNA Graph Code       33         Appendix F       TOPS1S Code       34     <	5	Task 3: Re-evaluation for Micron Tech., Inc.	17
5.1.1       Change in Facility Profit       17         5.1.2       Change in Restrictions       17         5.2       New Plan       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7       Conclusion and Evaluation       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.3       Evaluation of Strengths and Weaknesses       20         7.4       Evaluation and Evaluation       20         7.2       Conclusion       20         References       21         Appendix B       All learning Curves and Final DNA of Genetic Algorithm		5.1 Affected Factors	. 17
5.1.2       Change in Restrictions       17         5.2       New Plan       18         6       Task 4: Generalizability       18         6.1       Familiar Contexts       19         6.2       Land in Other Countries       20         7       Conclusion and Evaluation       20         7.1       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         7.2       Conclusion       20         7.2       Conclusion       20         7.2       Conclusion       20         7.4       Evaluation of Strengths and Weaknesses       20         7.2       Conclusion       20         References       20         Appendix A       Substantiating Tables and Data       22         Appendix B       All learning Curves and Final DNA of Genetic Algorithm       23         Appendix C       Genetic Algorithm Code       26         Appendix D       Genetic Algorithm DNA Graph Code       31         Appendix E       Linear Programming Code       33         Appendix F       TOPSIS Code       34		5.1.1 Change in Facility Profit	. 17
5.2 New Plan       18         6 Task 4: Generalizability       18         6.1 Familiar Contexts       19         6.2 Land in Other Countries       20         7 Conclusion and Evaluation       20         7.1 Evaluation of Strengths and Weaknesses       20         7.2 Conclusion       20         7.2 Conclusion       20         7.2 Conclusion       20         References       21         Appendix A       Substantiating Tables and Data       22         Appendix B       All learning Curves and Final DNA of Genetic Algorithm       23         Appendix C       Genetic Algorithm Code       26         Appendix D       Genetic Algorithm DNA Graph Code       31         Appendix F       TOPSIS Code       34		5.1.2 Change in Restrictions	. 17
6     Task 4: Generalizability     18       6.1     Familiar Contexts     19       6.2     Land in Other Countries     20       7     Conclusion and Evaluation     20       7.1     Evaluation of Strengths and Weaknesses     20       7.2     Conclusion     20       7.2     Conclusion     20       7.2     Conclusion     20       References     21       Appendix A     Substantiating Tables and Data     22       Appendix C     Genetic Algorithm Code     26       Appendix D     Genetic Algorithm Code     31       Appendix E     Linear Programming Code     33       Appendix F     TOPSIS Code     34		5.2 New Plan	. 18
6.1Familiar Contexts196.2Land in Other Countries207Conclusion and Evaluation207.1Evaluation of Strengths and Weaknesses207.2Conclusion20References21Appendix ASubstantiating Tables and Data22Appendix BAll learning Curves and Final DNA of Genetic Algorithm23Appendix CGenetic Algorithm Code26Appendix ELinear Programming Code33Appendix FTOPSIS Code34	6	Task 4: Generalizability	18
6.2Land in Other Countries207Conclusion and Evaluation207.1Evaluation of Strengths and Weaknesses207.2Conclusion20References21Appendix ASubstantiating Tables and Data22Appendix BAll learning Curves and Final DNA of Genetic Algorithm23Appendix CGenetic Algorithm Code26Appendix ELinear Programming Code33Appendix FTOPSIS Code34		6.1 Familiar Contexts	. 19
7     Conclusion and Evaluation     20       7.1     Evaluation of Strengths and Weaknesses     20       7.2     Conclusion     20       7.2     Conclusion     20       References       1     Appendix A     Substantiating Tables and Data     22       Appendix B     All learning Curves and Final DNA of Genetic Algorithm     23       Appendix C     Genetic Algorithm Code     26       Appendix D     Genetic Algorithm DNA Graph Code     31       Appendix E     Linear Programming Code     33       Appendix F     TOPSIS Code     34		6.2 Land in Other Countries	. 20
7.1 Evaluation 20   7.1 Evaluation of Strengths and Weaknesses 20   7.2 Conclusion 20   References 21   Appendix A Substantiating Tables and Data 22   Appendix B All learning Curves and Final DNA of Genetic Algorithm 23   Appendix C Genetic Algorithm Code 26   Appendix D Genetic Algorithm DNA Graph Code 31   Appendix E Linear Programming Code 33   Appendix F TOPSIS Code 34	7	Conclusion and Evaluation	20
7.1       Evaluation of Sterights and NetableSci 111111111111111111111111111111111111	1	71 Evaluation of Strengths and Weaknesses	20
References21Appendix ASubstantiating Tables and Data22Appendix BAll learning Curves and Final DNA of Genetic Algorithm23Appendix CGenetic Algorithm Code26Appendix DGenetic Algorithm DNA Graph Code31Appendix ELinear Programming Code33Appendix FTOPSIS Code34		7.2 Conclusion	. 20
References21Appendix ASubstantiating Tables and Data22Appendix BAll learning Curves and Final DNA of Genetic Algorithm23Appendix CGenetic Algorithm Code26Appendix DGenetic Algorithm DNA Graph Code31Appendix ELinear Programming Code33Appendix FTOPSIS Code34	_		
Appendix ASubstantiating Tables and Data22Appendix BAll learning Curves and Final DNA of Genetic Algorithm23Appendix CGenetic Algorithm Code26Appendix DGenetic Algorithm DNA Graph Code31Appendix ELinear Programming Code33Appendix FTOPSIS Code34	Re	ferences	21
Appendix BAll learning Curves and Final DNA of Genetic Algorithm23Appendix CGenetic Algorithm Code26Appendix DGenetic Algorithm DNA Graph Code31Appendix ELinear Programming Code33Appendix FTOPSIS Code34	A	opendix A Substantiating Tables and Data	22
Appendix CGenetic Algorithm Code26Appendix DGenetic Algorithm DNA Graph Code31Appendix ELinear Programming Code33Appendix FTOPSIS Code34	A	ppendix B All learning Curves and Final DNA of Genetic Algorithm	23
Appendix DGenetic Algorithm DNA Graph Code31Appendix ELinear Programming Code33Appendix FTOPSIS Code34	$\mathbf{A}_{j}$	opendix C Genetic Algorithm Code	26
Appendix ELinear Programming Code33Appendix FTOPSIS Code34	Aj	opendix D Genetic Algorithm DNA Graph Code	31
Appendix F TOPSIS Code 34	A	opendix E Linear Programming Code	33
••	A	opendix F TOPSIS Code	34

# 1 Introduction

**To build, or not to build: that is the question** that plagues land planners and decision makers day and night (and tomorrow, and tomorrow, and tomorrow). Regional planning is an extremely important aspect of land planning, and its importance has only increased in recent years as urban sprawl continues to grow [3]. On top of this, growing awareness over issues like climate change has caused land planners to become more mindful of how they design their plans, as well as what they should take into account during the design process. With this in mind, community leaders and business planners have consulted us to help decide the "best" use of a 3km<sup>2</sup> (741.316 acres) parcel of land 50 km away from Syracuse.

In this paper, we begin by creating a model to determine the "best" development option. Research is conducted to determine economic, environmental, and social criteria/sub-criteria with influence on development options. These variables are then applied in linear programming, TOPSIS, and genetic algorithm to create the base model. Next, by doing further research and collecting data, the model is applied to the parcel of land in New York. Sensitivity analysis is also conducted on the model to test the adaptability and reliability of its result.

We then explain how our model will be affected by the Micron Tech., Inc. fabrication facility being built not too far from the parcel of land. A new set of calculations are also performed for this scenario. Finally, the generalizability of our model is evaluated by discussing how it would perform in both an environment familiar to our team (Shenzhen, China) and in other international contexts.



Figure 1 Flow Chart of Process

# 2 Preliminary Assumptions and Definitions

# 2.1 Variable Definitions

Table 1	Variable Definitions	

Notations	Descriptions	Notations	Descriptions
Р	Annual profit	$O_i$	Facility <i>i</i> 's employment index
$A_i$	Attraction index of facility <i>i</i>	E	Annual carbon emission
$R_i$	Facility <i>i</i> 's recreational index	$S_i$	Facility <i>i</i> 's societal service index
$\alpha_i^{pr}$	Annual profit of facility <i>i</i>	$x_i^A$	Area of facility <i>i</i>
$\epsilon^{ce}_i$	Annual carbon emission of facility $i$	$x_b$	Highest annual profit possible
$y_b$	Least annual carbon emission possible	h	Developers' desired weighting
$A_{si}$	Facility $s$ 's area in land type $i$	F	Fixed cost
n	Number of Facilities	$A_{i}$	Area of facilities in land type $j$

### 2.2 Assumptions

Assumption 1: The "best" development option can be determined via purely quantitative means. This assumption is the basis of our model and also greatly simplifies it. Additionally, there are already many diverse quantitative measures available to employ in modelling, so limiting the factors used to quantitative ones will still provide a comprehensive result.

Assumption 2: All global, local, and environmental developments in the near and far future will not suddenly change and will remain relatively predictable. This includes extreme weather phenomena, sudden tragedies, and unforeseen economic and political changes. The nature of these things makes them unpredictable and rare, and therefore difficult - and arguably unnecessary due to their rarity - to model.

Assumption 3: The available budget for initial development is 50 million USD. Looking at land in and around Syracuse, even if we take the lower averages, this plot of land should cost far more than 50 million USD. Additionally, many of these development options require lots of money to build. Since these options have been considered by the decision-makers, it is reasonable to assume that we have at least 50 million USD to put towards developing this plot of land.

Assumption 4: The developments to be done on this land have been given the green light by the appropriate party (i.e. local or state government, permit association, etc.). Nearly all of the possible development options require some sort of building permit, development permit, or a similar green light. Thus, for the sake of being able to consider all of these options in our model, we assume that all possibilities have already received the necessary permits.

Assumption 5: The placement of land types is visually distinguishable and is as indicated in the provided satellite map. For the sake of simplicity and straightforwardness, we assume that the land types correspond with the visual cues in the satellite map; i.e., flat-looking yellow-green is cropland, an uneven patch of green is forest, etc.

Assumption 6: The best use of a cross-country skiing trail during the rest of the year is as a hiking trail. Cross-country skiing being only available for 3 months of the year gives this option a huge disadvantage, causing it to be automatically neglected by nearly any quantitative model. Thus, to level the playing field, we assume that the trail is open during the non-winter months as a hiking trail.

# 3 Task 1: Creating the Model

This task requires us to create a quantitative decision metric that can define the "best" use of the land. [6] To do this, we use a combination of **linear programming**, **TOPSIS**, and **genetic algorithm**:

- Linear Programming Used to obtain the maxima and minima of criteria [13]. We first use research to identify the most important criteria (in other words, the criteria that affect the development options the most). Then, formulae and restrictions are created to model these criteria in a standardized, quantitative way.
- **TOPSIS** We apply the maximum and minimum from linear programming to deduce the best overall alternative in TOPSIS [11]. By plotting each development option into the model and measuring distances between each option and the best/worst case, a "best" option (the option that is closest to the best case) is revealed.
- **Genetic Algorithm** Used to determine the distribution and location of facilities determined in TOP-SIS [9]. We invite the three "best" options (highest performing overall and by environmental and economic criteria) to participate in genetic modelling. Thus, the most ideal distribution for the land is finalized, and the "best" plan for the land is also finalized.

### 3.1 Initial Research

To conduct research, the sources consulted are largely government or official sources when possible (either Syracuse, New York State, or US National). If this is not possible, we look for data from relevant sources, such as solar panel companies for solar array information. Our data sources are listed in Table 2.

Information	Source	Site
Agricultural data: income, income:land trend	US Department of Agriculture	https://www.usda.gov
Geographical and Environmental data	City of Syracuse	https://www.syr.gov/Home
Economic information	Observatory of Economic Complexity (OEC)	https://oec.world
Solar Array information	LG Corporation	https://www.lg.com/global
income statistics	Forbes Finance Council	https://www.forbes.com
Agriculture finance information	Office of the New York State Comptroller	https://www.osc.state.ny.us
Carbon Emissions data	New York Academy of Sciences	https://nyaspubs.onlinelibrary.wiley.com
Agritrst, cross-country ski and crop info	Ontario Ministry (OMAFRA)	http://omafra.gov.on.ca

From this research, seven factors stand out as criteria that would affect the determination of the "best" development option: profit, employment opportunities, attraction of tourism, carbon emissions, environmental degradation, recreational offers, and societal benefits.

### 3.2 Criteria Identification

The final determined criteria can largely fit into three main categories: economic, environmental, and social, as is shown in Figure 2.



Figure 2 Quantitative Criteria

- Economic Factors:
  - **Profit:** Referenced by *P*. This includes the profit generated by all facilities while extracting the cost required to produce goods or services with respect to time and area coverage.
  - **Employment Opportunities:** Referenced by *O<sub>i</sub>*. This is an evaluative index on the employment opportunities provided by land development *i*.
  - Attraction of Tourism: Referenced by A<sub>i</sub>. This is an evaluative index on the tourist and resident attraction value of development *i*. An increase in the attraction will certainly be a booster to the local and possibly even the state economy.
- Enviromental Factors:
  - Carbon Emissions: Referenced by *E*. It is essential to minimize carbon emissions because they contribute to climate change that poses a significant threat to the environment, economy, and human societies worldwide.
  - Environmental Degradation: Referenced by  $E_W$ ,  $E_F$ ,  $E_D$ , and  $E_C$ . This is a penalty-based index utilized in the genetic algorithm. It considers the effect of biodiversity reduction, soil erosion, and all forms of pollution on each land type.
- Social Factors:
  - Recreation: Referenced by *R<sub>i</sub>*. Citizens' enjoyment will also matter in this deciding factor. Some facilities offer recreational activities, while others do not. That will affect the locals' acceptance of the facilities and thus affect aspects such as attraction of tourism and employment opportunities.

- Societal Benefits: Referenced by  $S_i$ . Other than recreation, there are also other facilities that a society yearns, might that be education, clean water, nutritious crops, or other similar aspects.

#### 3.3 Linear Programming for Preliminary Planning

In the first step of this model, linear programming is used to incorporate criteria that can be modelled linearly. These criteria can be either objective functions to be maximized or minimized, or restrictions on those functions. The variables involved are assumed to be continuous. The resulting solution is definitive and represents the best possible solution, given the available resources and restrictions imposed.

To facilitate the chosen criteria in linear programming, social factors are incorporated into restrictions on economic and environmental. In other words, they are not independent objective functions that need to be optimized.

#### 3.3.1 Economic

In modelling the aforementioned economic criteria in linear programming, the profit should be maximized. The development option that yields the highest economic results should be the "best" in that aspect, as it would have the highest profit, provide the most employment opportunities, and attract the most tourists and residents.

$$\max P = \sum_{i=1}^{n} \left( \alpha_i^{pr} \times x_i^A \right) \tag{1}$$

$$s.t. \begin{cases} \sum_{i=1}^{n} x_i^A \le 741.316\\ \sum_{i=1}^{n} S_i \times x_i^A \ge 3000\\ \sum_{i=1}^{n} R_i \times x_i^A \ge 2000\\ \sum_{i=1}^{n} O_i \times x_i^A \ge 4500\\ \sum_{i=1}^{n} A_i \times x_i^A \ge 1500 \end{cases}$$
(2)

where *P* is the profit;  $\alpha_i^{pr}$  is the annual profit of facility *i*;  $x_i^A$  is the area of facility *i* in acres;  $S_i$  is the societal index of facility *i*;  $R_i$  is the recreational index of facility *i*;  $O_i$  is the employment opportunity index of facility *i*; and  $A_i$  is the tourism and residence attraction index of facility *i*.

#### **Restriction Explanation**

- $\sum_{i=1}^{n} x_i^A \leq 741.316$ : As a basic measure, the first restriction placed on this confirms that the facility does not exceed the available area of land.
- ∑<sub>i=1</sub><sup>n</sup> O<sub>i</sub> × x<sub>i</sub><sup>A</sup> ≥ 4500 and ∑<sub>i=1</sub><sup>n</sup> A<sub>i</sub> × x<sub>i</sub><sup>A</sup> ≥ 1500: Restrictions are also written to ensure that employment opportunities (O<sub>i</sub>) and attraction of tourism (A<sub>i</sub>) are sufficient enough to provide tangible economic benefits.
- $\sum_{i=1}^{n} S_i \times x_i^A \ge 3000$  and  $\sum_{i=1}^{n} R_i \times x_i^A \ge 2000$ : Finally, the societal factors are incorporated into the restrictions.  $\sum_{i=1}^{n} S_i \times x_i^A \ge 3000$  sets the bar for societal benefits to the local community, and  $\sum_{i=1}^{n} R_i \times x_i^A \ge 2000$  for recreational opportunities.

#### 3.3.2 Environmental

The environmental criteria - only carbon emissions in this case - should be as low as possible (i.e. minimized) to deduce the "best" option under this criteria.

$$\min E = \sum_{i=1}^{n} \left( \epsilon_i^{ce} \times x_i^A \right) \tag{3}$$

$$s.t. \begin{cases} \sum_{i=1}^{n} x_i^A \le 741.316\\ \sum_{i=1}^{n} S_i \times x_i^A \ge 3000\\ \sum_{i=1}^{n} R_i \times x_i^A \ge 2000 \end{cases}$$
(4)

where *E* is the annual carbon emission of the land model in *kg*; and  $\epsilon_i^{ce}$  is the annual carbon emission of facility *i* in  $kg \cdot acres^{-1}$ .

#### **Restriction Explanation**

Because there is only one environmental factor being modelled with linear programming, the restrictions are comprised of only

- $\sum_{i=1}^{n} x_i^A \leq 741.316$  the basic area restriction, and
- $\sum_{i=1}^{n} S_i \times x_i^A \ge 3000$  and  $\sum_{i=1}^{n} R_i \times x_i^A \ge 2000$ , the societal restrictions, as described previously.

### 3.4 TOPSIS for Working Model

With a finished linear programming model, we can begin to use TOPSIS to create a working model that can define the one "best" alternative.

#### 3.4.1 Introduction to TOPSIS

TOPSIS (Technique for Order of Preference by Similarity to Ideal Solution) [2] is a multi-criteria decisionmaking method used to evaluate the best alternative from a set of available options. It is based on the assumption that the best alternative is the one that has the shortest distance from the positive ideal solution (i.e. the best alternative that maximizes the criteria) and the longest distance from the negative least ideal solution (i.e. the worst alternative that minimizes the criteria).

To apply the method, a set of criteria is first defined. Weights are then assigned to each criterion based on the criterion's relative importance. Then, a matrix including each alternative and criterion is constructed. The matrix is also normalized to account for differences in the scale of the criteria. Finally, the distance between each alternative and the best and worst solutions is measured, and the alternatives are ranked based on their closeness to the positive ideal solution.

#### 3.4.2 TOPSIS in Our Model

The TOPSIS model in this report will be done on a 2D coordinate plane, with the x-axis measuring annual economic profit and the y-axis measuring annual carbon emissions, as calculated in the linear programming section.

1. Normalization: The x value  $x_b$  represents the highest annual , and the y value  $y_b$  represents the least annual carbon emission. It must also be considered that the range of profits could be drastically different from the range of carbon emissions. To standardize the relationship between the two, the environmental value will be modified (multiplied by r) to emulate the former.

$$\frac{|x_b|}{|y_b|} = r \tag{5}$$

- 2. Weighting: To weigh the economic and environmental factors according to their influence, the economic aspect will also be adjusted to be h times that of the environmental, if the decision maker so wishes (if not, then h = 1). This is proposed to account for the fact that each stakeholder will have different beliefs as to which factors are more important in determining the "best" development option.
- 3. **Best and Worst:** Taking into account these preliminary factors, a formula is created to determine the best (positive ideal) and worst (negative least ideal) possibilities *I*<sub>b</sub> and *I*<sub>w</sub>, respectively:

$$I_b = (x_b|h \times \max(P), y_b|r \times \min(E)), \quad I_w = (x_w|h \times \min(P), y_w|r \times \max(E))$$
(6)

4. **Candidates Selection:** To reduce the time complexity of the model, 19 points are then manually determined, of which we believe at least one must be the best option. These points are set on a spectrum, ranging from heavily considering environmental factors (5:95%) to heavily considering economic factors (95:5%). The 19 points  $(x_{\omega}, y_{\omega})$  are each determined using another linear programming system that combines economics and environment considerations.

$$\max \sum_{i=1}^{n} x_{i}^{A} \left( h \times \omega \times \alpha_{i}^{pr} - r \times (1 - \omega) \times \epsilon_{i}^{ce} \right)$$

$$s.t. \begin{cases} \sum_{i=1}^{n} x_{i}^{A} \leq 741.316 \\ \sum_{i=1}^{n} S_{i} \times x_{i}^{A} \geq 3000 \\ \sum_{i=1}^{n} R_{i} \times x_{i}^{A} \geq 2000 \\ \sum_{i=1}^{n} O_{i} \times x_{i}^{A} \geq 4500 \\ \sum_{i=1}^{n} A_{i} \times x_{i}^{A} \geq 1500 \end{cases}$$
(8)

where  $\omega \in \{0.05, 0.1, 0.15, \dots, 0.95\}$ . From the aforewritten formulae, the calculation for  $x_{\omega}$  and  $y_{\omega}$  can be formed:

$$x_{\omega} = h \times \sum_{i=1}^{n} x_i^A \alpha_i^{pr}, \ y_{\omega} = r \times \sum_{i=1}^{n} x_i^A \epsilon_i^{ce}$$
(9)

5. **Distance Calculation:** Finally, with  $x_{\omega}$  and  $y_{\omega}$ , distance calculations - the defining aspect of TOPSIS - begin. Using the distance formula, the distance between development option  $\omega$  at  $(x_{\omega}, y_{\omega})$  and the ideal and least ideal possibilities are calculated as

$$d_{\omega w} = \sqrt{(x_{\omega} - x_b)^2 + (y_{\omega} - y_b)^2}, \quad d_{\omega b} = \sqrt{(x_{\omega} - x_w)^2 + (y_{\omega} - y_w)^2}.$$
 (10)

6. Judging Index Calculation: Both distance calculations are repeated for all 19 manually-determined points established above. After the process is finished and results are recorded, a judging index  $s_{\omega}$  is created based on the distance of point each point  $(x_{\omega}, y_{\omega})$  from the ideal and least ideal possibilities:

$$s_{\omega} = \frac{d_{\omega w}}{d_{\omega w} + d_{\omega b}}, 0 \le s_{\omega} \le 1.$$
(11)

Note that  $s_{\omega} = 1$  if and only if the option is exactly the ideal alternative, and  $s_{\omega} = 0$  if and only if the option is exactly the least ideal alternative.

7. **Ranking:** All results are taken and ranked according to  $s_{\omega}$ , and the highest ranking overall option is chosen along with the highest-performing economic and environmental options from linear programming to participate in the next step, genetic algorithm (GA).

### 3.5 Genetic Algorithm (GA) for Application

Next, the positioning of each facility must be calculated. This is because, although the maximum profit of different facilities have now been shown, it is still necessary to evaluate their placement for minimum environmental damage according to the environmental degradation criteria determined in Section 3.2.

#### 3.5.1 Process of Genetic Algorithm

GA is a type of optimization algorithm that uses a heuristic search technique, finding the optimal solution to a given problem by mimicking the process of natural selection and evolution. Genetic algorithm goes through the following steps to achieve this:

- **Initialization**: First, a possible solution (the initial instance) is found and fed to the program in the form of **"DNA"**, a binary sequence indicating all the required input, just like all the other generations. The DNA data is a string that constrains all variable subject to change,
- **Conversion**: The binary sequence in the DNA is converted to decimal variables, and fitted across the range of all possible data.
- **Selection**: The **"fitness"** of the DNA is evaluated based on how successful it is in solving the objective function. If the DNA sequence has a high fitness value, it gets a higher chance to survive and reproduce the next generation of offspring.
- **Reproduction**: This is done through **crossover**, where one parent selected according to fitness has its DNA replaced at random points by another randomly selected parent.
- **Mutation**: During this process, mutations may occur by arbitrarily choosing a DNA bit from a child and reverting it.
- **Repetition until convergence**: The steps described above are repeated for a fixed number of generations (at which point the final-generation child with the highest fitness is selected), or indefinitely until the satisfactory solution is found.

GA is particularly suitable for problems that involve non-linear objective functions and large solution spaces, and the detail of GA is shown in Algorithm 1.

```
Algorithm 1: Genetic Algorithm for Finding Best Solution
   Input: An instance \delta, DNA length \beta, reproduction rate \alpha, mutation rate \gamma, population size
            \sigma, generation number \omega
   Output: Fittest DNA string found P<sub>best</sub>
   // Initialize
1 Objective function OF(x), Current Population P, Current Fitness F;
<sup>2</sup> Generate \sigma DNA genes, each being 60 bytes long, and save them to P;
3 for i \leftarrow 0 to \omega do
       // Calculate Fitness
       for j \leftarrow 0 to \sigma do
4
        F[j] \leftarrow OF(P[j]);
 5
       // Selection according to Fitness
       for j \leftarrow 0 to \sigma do
6
           Choose DNA P[\theta] with replacement Rwith probability^{F[\theta]} / \sum_{k=1}^{\sigma-1} F[k];
 7
           Randomly choose DNA P[\kappa] with replacement;
 8
           // Reproduction
           if randint \in [0, 1] \leq \alpha then
 9
               Randomly choose k;
10
               set P[\theta][k] \leftarrow P[\kappa][k];
11
       // Mutation
       for j \leftarrow 0 to \sigma do
12
           for k \leftarrow 0 to 60 do
13
               if randint \in [0,1] \leq \gamma then
14
                    Revert P[j][k] from 0 to 1 or from 1 to 0;
15
   // Return
16 return P_{best} \leftarrow \max F_i;
```

#### 3.5.2 Application of Genetic Algorithm

To simplify the model, we put the map into a flat Cartesian coordinate system. Assume that the point at the bottom left corner of the map is the origin point (0,0), and the top right corner will be (20, 17.5). Hence, each unit of land is calculated to be equal to  $\frac{Area_{land}}{Area_{plane}} = 2.709$  acres of land.

Since the profit of the facilities is constant with the calculated area of TOPSIS, the genetic algorithm will focus on an aspect called **opportunity cost**. Opportunity cost is defined as the loss of potential gain from other alternatives when one is chosen. In our model, this cost is a number between 0 to 30, with a lower number indicating a more precious environment.

The opportunity cost [10] of each land type is formed by 3 different aspects - Pollution, Soil Erosion, and Biodiversity. Each has their specific environment cost (except shrubs, which will not be considered due its mere one percent coverage).  $E_W$  represents the environmental cost of wetland;  $E_F$  of forest;  $E_D$  of developed land; and  $E_C$  of crop land.

The objective function - the fitness evaluator - is as follows:

$$\max \sum_{m \in \mathcal{S}} A_m E_m \tag{12}$$

$$s.t. \begin{cases} |x_{si} - x_{sj}| \ge \frac{\Delta x_{si} + \Delta x_{sj}}{2} \\ |y_{si} - y_{sj}| \ge \frac{\Delta y_{si} + \Delta y_{sj}}{2} \\ (x_{si} \pm \Delta x_{si}, y_{si} \pm \Delta y_{si}) \in M \\ (x_{si} \pm \Delta x_{si}, y_{si} \mp \Delta y_{si}) \in M \end{cases}$$

$$(13)$$

where *m* is the land type; *s* is the type of facility;  $k_s$  is the number of facility *s*;  $A_s i$  refers to the area of facility *s* in land type *i*; *S* is the set of {*Wetland*, *Forest*, *Developed*, *Crop*}; and ( $x_{si}, y_{si}$ ), ( $x_{sj}, y_{sj}$ ) is the center of the facilities (assuming all facilities are rectangular with sides parallel to either the x-axis or y-axis). Note that in programming, the input is taken in the bottom left corner, and the center is then calculated by adding half of the height and width.  $\Delta x_{si}$  is the width of the rectangle and  $\Delta y_{si}$  is the length; and  $A_W, A_F, A_D, A_C$  refers to the area of facilities in wetland, forest, developed area, and cropland, respectively.

#### **Restrictions Explanations**

- $|x_{si} x_{sj}| \ge \frac{\Delta x_{si} + \Delta x_{sj}}{2}$  and  $|y_{si} y_{sj}| \ge \frac{\Delta y_{si} + \Delta y_{sj}}{2}$  ensure that the facilities do not overlap with each other, and
- $(x_{si} \pm \Delta x_{si}, y_{si} \pm \Delta y_{si}) \bigcup (x_{si} \pm \Delta x_{si}, y_{si} \mp \Delta y_{si}) \in M$  ensures that the facilities lie inside the map.

The detail of the results is further explained in Section 4.2.3, and the complete code for GA is demonstrated in Appendix C.

#### 3.6 Short- and Long-term Considerations

To incorporate the short-term and long-term into consideration, we focus on **total profit**, which is equal to the total production value minus the total cost. In other words, the total profit of a certain distribution of facilities will be equal to the total cost of maintenance subtracted from the value of all goods produced in a year. Thus, to find total profit, the equation

$$T_p(t) = P(t) - C(t)$$
 (14)

is used, where  $T_p(t)$  is the total profit; P(t) is total production value accumulated through t years; and C(t) is total cost accumulated through t years.

• Total Production: The total production value can be measured by the convolution of the Cobb-Douglas production function [8] and an exponential function:

$$P(t) = Y(t) * (1+\alpha)^{t} = \int_{0}^{t} Y(u)(1+\alpha)^{t-u} du$$
(15)

where  $\alpha$  is the rate of inflation. Y(t) is the Cobb-Douglas production function

$$Y(t) = A \times L(t)^g \times K(t)^j$$
(16)

where A is the efficiency constant; g and j are economic constants. The efficiency constant is a measure of total factor productivity. The economic constant measures the output elasticity (percentage change of output) of capital and labour.

Additionally, L(t) is the total labour with respect to time, where labour is the working time. L(t) can be expressed as

$$L(t) = -\frac{a(L_i - L_0)}{t + a} + L_i$$
(17)

where *a* is the labour constant;  $L_0$  is the total hours of labour at t = 0;  $L_i$  is the total hours of labour at  $t = \infty$ .

K(t) is the total capital with respect to time, which can be expressed as

$$\begin{cases} \frac{\mathrm{d}K}{\mathrm{d}t} = r(1 - \frac{K}{K_i})K\\ K(0) = K_0 \end{cases}$$
(18)

where *r* is the growth constant;  $K_0$  is the total hours of labour at t = 0; and  $K_i$  is the total hours of labour at  $t = \infty$ . The growth constant is a measure of the speed at which facility construction is completed.

From this, the solution to the function is concluded to be:

$$K(t) = \frac{K_i}{1 + (\frac{K_i}{K_0} - 1)e^{-rt}}$$
(19)

• Total Cost: The total cost consists of the fixed cost (cost to build) and the accumulated operating cost (cost of maintenance and operations). The operating cost can be measured by the convolution of a logarithmic function and an exponent function. The total cost function C(t) is:

$$C(t) = F + \log(bt+1) * (1+\alpha)^{t} = F + \int_{0}^{t} \log(bu+1) (1+\alpha)^{t-u} du$$
(20)

where F is the fixed cost; and b is a constant.

• **Total Profit**: Plug all functions K(t) and C(t) into the main function, and the result will be:

$$T_p(t) = A \int_0^t \left( -\frac{a(L_i - L_0)}{t + a} + L_i \right)^g \left( \frac{K_i}{1 + (\frac{K_i}{K_0} - 1)e^{-rt}} \right)^j (1 + \alpha)^{t - u} \mathrm{d}u - F - \int_0^t \log\left(bu + 1\right) (1 + \alpha)^{t - u} \mathrm{d}u$$
(21)

From this, the function can be graphed and visualizations can be made for the short-term and long-term profit fluctuation based on labour input, capital input, inflation rate, and fixed cost. The numerical solution and the detail of results are further explained in section 4.2.4.

# 4 Task 2: Application and Sensitivity Analysis

We first revisit the sources listed under Section 3.1 and gather concrete data to incorporate into the finished model. From this, the "best" options out of those listed by the decision-makers are determined using linear programming and TOPSIS. Their positioning is also calculated using genetic algorithm. The short- and long-term profit analysis is then applied on the genetic algorithm results. Finally, a sensitivity analysis is conducted on our model to evaluate its reliability and the sensitivity of the results.

### 4.1 Data Collection

Using the sources listed in Table 2, we determined concrete numbers for each variable and each development option. Our final master data table with all of these values can be seen in Table 3.

Measurement	Sports Comp.	Ski/Trail	Crop F.	Ranch	Regen. F.	Sol. Arr.	Agritrst Cn.	Agrvltc F.
$P_j$ (\$ · acre^{-1})	9038.46	254.95	179.28	562.51	319.30	19155.41	3999.91	215.09
$E_j (kg \cdot acre^{-1})$	200	50	-25	500	-20	-3330	-2	-2030
$O_i$	9.5	1.0	7.5	8.5	8.5	2.5	9.0	7.5
$A_i$	9.5	8.0	1.0	1.0	1.5	1.0	7.0	1.0
$S_i$	3.0	4.0	8.0	9.0	9.0	3.0	6.0	7.0
$R_i$	10.0	9.0	1.0	2.0	2.0	1.0	9.0	2.0

 Table 3
 Data of Different Facilities

The Employment Opportunity Index  $O_i$ , Tourism Attraction Index  $A_i$ , Societal Benefit Index  $S_i$ , and Recreational Index  $R_i$  are all determined manually as a number from 1.0 to 10.0 via a thorough analysis of all available sources on each respective topic. The environmental degradation penalties  $E_W$ ,  $E_D$ ,  $E_F$ , and  $E_C$  are also determined using this method. The exact values can be seen in Table 14. Additionally, the carbon emission data  $E_j$  are all rounded to the nearest integer.

### 4.2 The "Best" Option

The data described above are applied to the linear programming systems defined in Section 3.3, the TOP-SIS process in Section 3.4, and the genetic algorithm introduced in Section 3.5. In this way, the "best" land development options and their distribution and positioning are determined.

#### 4.2.1 Linear Programming Results

Using the linear programming systems defined in Section 3.3 and the data described in Section 4.1, results for the economic and environmental criteria are calculated.

The optimal result with maximum annual profit, at \$9 079 300, can be seen in Table 4; and the optimal result with minimum annual carbon emissions, at -1 869 100kg, can be seen in Table 5. These two results will advance to be employed in the genetic algorithm analysis.

The calculated minima for both economic and environmental have also been listed in these two tables. The two minima are used to calculate the least ideal possibility in TOPSIS.

Facilities	Sports Comp.	Ski/Trail	Crop F.	Ranch	Regen. F.	Sol. Arr.	Agritrst Cn.	Agrvltc F.
Economic Ideal (acres)	267	0	0	129	0	344	1	0
Economic Least Ideal (acres)	0	158	579	0	0	0	0	0

Table 4 Economic Max./Min. Facilities (\$9079300 and \$144090 in Annual Profit)

Table 5         Environmental Min./Max. Facilities (-1869100)	kg and +351000kg Annual CO <sub>2</sub> Emissions)
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Facilities	Sports Comp.	Ski/Trail	Crop F.	Ranch	Regen. F.	Sol. Arr.	Agritrst Cn.	Agrvltc F.
Environment Ideal (acres)	0	0	0	0	0	510	147	84
Environment Least Ideal (acres)	65	0	0	676	0	0	0	0

#### 4.2.2 TOPSIS Results

These results are then applied to the TOPSIS model described in Section 3.4. We first set r to 4.86 to standardize the relationship between environmental and economic based on the ranges found in the data.

$$\frac{|x_b|}{|y_b|} \approx 4.86\tag{22}$$

h is also set to 2, making the final ratio/weighting between environmental to economic factors 1 : 2. This is because we believe that, although environment is a very important factor, comparing solely carbon emissions to the entirety of all the economic benefits would be an unfair comparison. There are 3 economic factors and 1 environmental, so a 1-env. to 2-econ. weighting would best reflect our beliefs.

With *r* as 4.86 and *h* as 2, the coordinates of the ideal possibility are  $A_b = (18158600, -9083826)$  and the coordinates of the least ideal possibility are  $A_w = (288180, 1705860)$ .

Next, the 19 manually determined points are plotted into TOPSIS and ranked according to  $\omega$ , the result of which can be seen in Table 6 below.

Table 6	Alternatives Acc	ording to J	udging Ind	dex $s_{\omega}$ ; ranked	best-worst
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Weighting	0.95 - 0.45 Econ.	0.4 Econ.	0.35 - 0.25 Econ.	0.2 Econ.	0.15 - 0.1 Econ.	0.05 Econ.
Index $\omega$	0.463650	0.457908	0.457321	0.431908	0.431316	0.430778

The top performing development option from TOPSIS, which will be modelled in GA along with the two aforementioned results from linear programming, can be seen in Table 7. This option, with an annual profit of \$9047920 and annual CO<sub>2</sub> emissions of -1094700 kg, is found at 0.95 - 0.45 Econ.

 Table 7
 Distribution of Top Option, according to TOPSIS

Facilities	Sports Comp.	Ski/Trail	Crop F.	Ranch	Regen. F.	Sol. Arr.	Agritrst Cn.	Agrvltc F.
Best Option (acres)	267	0	0	0	129	344	1	0

#### 4.2.3 Genetic Algorithm Results

We then use the genetic algorithm to determine the positioning of facilities for each of the three ideal results. This is done by following the GA process as is described in Section 3.5.



Figure 3 The Annotated and Plotted Map of All Land Types

• **Cartesian coordinate system:** The map is first plotted in the 2D Cartesian plane. The placement and area of each land type is assumed from the given satellite map view and outlined using rectangles.

The distribution of each land type except forest is as follows; the forest is the remainder of the area. A limitation of this approach is the inability to accurately note the environment with rectangles, especially when this map isn't very visually distinguishable.

The tables in Appendix A specify the exact (x, y) coordinates of each rectangle's diagonal vertices.

- Initialization: As described in Section 3.5.1, all inputs are fed to the genes in the form of DNA which, in our instance, contains the lower left corner and width of the rectangles. This is the only information needed to calculate the length of the rectangle with its area predetermined.
- **Conversion:** In this model, the DNA is 60 bits long. It is separated into 12 sections, each with a length of 5, storing data up to 31. The first 4 sets of 5 (the first 20) manifest the x coordinate of the rectangle's bottom left vertex. The second 20 are similar but for y; and the last 20 are indications of the width of each facility.

Figure 4	An Example of DNA	String
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#### • Objective Function Constraints:

- No Overlaps: The overlapping area function is created in accordance with the restrictions described in Section 3.5.2 ensuring that facilities do not overlap with each other. To follow the restriction, the code will ensure the overlapping area between two rectangles is 0. The overlapping area code can be seen in lines [31~49] of Appendix C.
- No out-of-bounds: To ensure that land developments lie within the boundary, new restrictions are set to ensure:
  - (a) the lower left corner of a facility does not exceed the hypotenuse of the lower left triangle;
  - (b) the upper right corner does not exceed the hypotenuse of the upper right triangle.

Both triangles are shown in pink in Figure 3. To incorporate this into the objective function, two linear inequalities are used. Let (x, y) be the lower left corner, A be area, and w be width. This gives the equation of the lower left hypotenuse as  $y = \frac{-8.5}{6}x + 8.5$  and the equation of the upper right hypotenuse as  $y = \frac{-7.5}{4.5}x + 44.33333$ . The constraints are thus:

$$y \ge \frac{-8.5}{6}x + 8.5$$

$$y + \frac{A}{w} \le \frac{-7.5}{4.5}(x+w) + 44.33333$$
(23)

If any of the constraints are not met by a string of DNA, then it is immediately abandoned with its fitness set to 0. Otherwise, if a string of DNA meets all of the constraints, its fitness value is calculated according to the objective function (see line [ $84 \sim 224$ ] of Appendix C).

- **Objective Function:** Table 14 lists the values of the environmental degradation penalties  $E_W$ ,  $E_D$ ,  $E_F$ , and  $E_C$  to be employed in the objective function. To maximize the fitness of the DNA, the environmental degradation factor should have an inverse relationship with the preciousness of the environment. Thus, the environmental factor is 30 total.
- Selection, Reproduction, and Mutation: DNA sequences then undergo the process of Genetic Algorithm as written in Section 3.5. Their code appears in Appendix C.
- Additional Variable Occupation Rate: Since TOPSIS grants the ratio between areas, there is one more variable called occupation rate that must be decided by the decision makers. This variable dictates the proportion of the total land area the development is going to occupy. Let this variable be named *γ*. Then:

$$A_{cordinate} = A_{acres} \times 2.709\gamma.$$
<sup>(24)</sup>

• **Application:** The initial instance is generated in two ways, either randomly generated or hand-drawn. With a lower occupation rate, random generation will be faster; but, when the occupation rate is 0.5 or higher, hand-drawing will be more efficient. To verify and debug the initial and final DNA, the facilities are graphed according to the DNA string (see Appendix B).

GA also relies on user inputs to determine the size of the DNA (choice and justification described above), population, crossover rate, and more. These are all determinate factors to the success of the generation since the genetic algorithm only promises the maximum to the highest extent of convergence given the user inputs. The user inputs used in our instance are listed below.

Table 8	User Inputs
Iuvic o	

DNA size	Population	Cross Rate	Mutation Rate	Generations	width/x/y bounds
60	1000	0.8	0.002	400	[1,20] [0,20] [0,17.5]

• **Results:** With the aforementioned user inputs, the genetic algorithm runs across three different occupation rates throughout the three different models of facilities proposed by TOPSIS and linear programming.

 Table 9
 Resulting Fitness of All 3 Cases, calculated via objective function

Occupation rate	TOPSIS Best	Economic Best	Environmental Best
0.4	1620.07338413	1246.89606331	1530.62376101
0.5	1899.65084277	1473.23451274	1761.06401523
0.6	2020.18783949	1455.66527764	1996.19740878

The distribution of facilities on the land, as calculated from the TOPSIS Best option at an occupation rate of 0.5, is provided in Figure 5. The result's DNA string, graph, and converted DNA, among others, are listed in Table 10. Similar maps and tables can be seen for the rest of the results in Appendix B. The overall evaluation of the proposed land planning and allocation is in Figure 6.





**Figure 5** Map of GA Best Option with 0.5 Occupation Rate

Figure 6 Evaluation Result



Occupation rate	Fitness	Best DNA string	Learning Curve	Converted DNA string in the form of [x, y, width]
0.5	1899.7	$\begin{array}{c} 0 \ 1 \ 1 \ 0 \ 1 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 1 \\ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 0 \ 1 \\ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 1 \ 1 \ 1 \ 0 \ 1 \\ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 1 \\ \end{array}$	1900 1850 1900 1750 1750 100 150 0 50 100 150 200 250 300 350 400	Sports Complex:[7.7, 7.9, 5.2] Regen. Farm: [0.0, 11.9, 7.7] Solar Array: [6.5, 0.0, 12.9] Agritourist C.: [19.1, 8.5, 0.6]

#### 4.2.4 Short- and Long-term Results

After applying all the obtained data into Equation (21) in Section 3.6, the function of total profit is:

$$T_p(t) = A \int_0^t \left( -\frac{500}{t+10} + 50 \right)^{0.3} \left( \frac{30}{1 + (\frac{30}{2.6} - 1)e^{-t}} \right)^{0.7} (1+\alpha)^{t-u} \mathrm{d}u - 30 - \int_0^t \log\left(12u + 1\right) (1+\alpha)^{t-u} \mathrm{d}u$$
 (25)

where  $\alpha$  is the inflation rate and A is the efficiency constant that measures the ratio of output and input of labour and capital, respectively. In figure 7, the projected futures include three varieties: best-case, expected, and worst-case futures. These projections are determined by adjusting the aforementioned constants (A and  $\alpha$ ).



Figure 7 The Projected Future

In the short term, profits for all cases will be negative as construction costs must be covered, but the production value is limited due to less labour and capital input. However, in the long term, profits will grow from inflation rates and high production value. Better case scenarios project higher profits.

The best-case scenario predicts that fixed costs will be covered in year 15, resulting in a total profit of 43 million by year 25 and 261 million by year 50. The expected future, calculated using the most likely inflation and efficiency values, forecasts that fixed costs will be covered in year 16, leading to a total profit of 28 million by year 25 and 138 million by year 50. In the worst-case scenario, fixed costs won't be covered until year 42, and the total profit will be 7 million by year 50. Despite this, however, the results of the model are considered dependable profit-wise because even the worst-case scenario yields a positive total profit within 50 years.

# 4.3 Sensitivity Analysis

Sensitivity analysis must be conducted to assess the degree of uncertainty and variability and to identify the parameters that have the greatest impact on the results. This information can then be used to refine the model, optimize its parameters, or identify areas where further data collection may be needed.

#### 4.3.1 Sensitivity Analysis of Linear Programming

There are two aspects that can be tested and manipulated to conduct a sensitivity analysis [4] of linear programming: **tight constraints** [1] and **shadow price** [7].

**Tight restrictions** refer to constraints that are met with equality in the objective value, thus limiting it. The restrictions in linear programming will always form a convex polygon, and the objective function is, in essence, another line on the coordinate plane. To obtain the most optimal value, the objective function will always intersect the polygon at one of its corners. Tight restrictions are the inequalities, which, when plotted on the coordinate plane, form the corner intersected by the objective function. On the other hand, loose restrictions are those that do not influence the result whatsoever. Nonetheless, the polygon might shift in shape, thus altering the tight or loose status of the restrictions.

**Shadow price** refers to the change in the objective value that results from a change in the range of the tight restrictions. As previously mentioned, tight restrictions are those that form the corner that will be intersected by the objective function to reach the optimal solution. Thus, any change in their range will result in a return value dependent on the magnitude of the change.



Figure 8 Linear Programming Demonstration in 2D; image taken from [5]

**Tight constraints and shadow price** are calculated for both the environmental and economic linear programming systems. First, for the **environmental linear programming system**, there are three restrictions tested as tight constraints. They are as follows:

- 1. the basic area restriction  $\sum_{i=1}^{n} x_i^A \leq 741.316$ ;
- 2. the societal benefit index restriction  $\sum_{i=1}^{n} S_i \times x_i^A \ge 3000$ ;
- 3. the recreation index restriction  $\sum_{i=1}^{n} R_i \times x_i^A \ge 2000$ .

As is shown in Figure 9, the sensitivity analysis graph for the area restriction shows a linear decrease in the range observed (67.5% to 132.5%), suggesting that as the restrictive range increases, the carbon emissions decrease. At 67.5%, the restrictions oppose each other, making further optimization impossible.

The sensitivity analysis graph for societal benefit restrictions is piece-wise, comprising three distinct regions with different slopes. The slope of 0 at the first part (50% to 74.5%) indicates a loose restriction before 74.5%. The second part's positive slope indicates the return value from a percentage increase is unfavorable. The third phase has a steeper slope, demonstrating a more unfavorable return value.

The sensitivity analysis graph for recreational opportunity restrictions is also piece-wise, with an almost unnoticeable increase in the slope at the 140.5% point. Overall, it demonstrates unfavourable return values for percentage increases in the constraining constant.



Figure 9 Sensitivity Analysis and Shadow Prices for Environmental Linear Programming System

In the economic linear programming system, the restrictions tested as tight constraints include:

- 1. the basic area restriction  $\sum_{i=1}^{n} x_i^A \leq 741.316$ ;
- 2. the societal benefit index restriction  $\sum_{i=1}^{n} S_i \times x_i^A \ge 3000$ ;

3. the third restriction, which is not recreation index, but rather the employment opportunity index restriction  $\sum_{i=1}^{n} O_i \times x_i^A \ge 4500$ .

As can be seen in Figure 10, these graphs almost exactly mirror the shadow price graphs of the environmental tight constraints. Where decreases were seen previously, increases are seen here, and vice-versa. However, there are still a few exceptions.

- In the societal restriction of the economic section, the graph exhibits a longer second phase with a steeper slope in addition to a smoother transition from phase 2 to 3.
- The economic employment opportunity sensitivity graph is utterly distinct from the environment's recreation restriction. This graph has a slope of 0 from 50% to 69.5%, indicating a loose restriction status there. After that, however, it has a sustained slope inside the observed range, with a direct relationship between the decrease in profit and the increase in the constraining constant.



Figure 10 Sensitivity Analysis and Shadow Prices for Economic Linear Programming System

In conclusion, to reduce carbon emissions, either societal or recreational constraining constants should be decreased, or area constraining constants should be increased. To increase profits, societal and employment opportunity constraining constants should be decreased, or area constraining constants should be increased. However, adjusting these factors would reduce the respective benefits provided by the land.

#### 4.3.2 Senstivity Analysis of TOPSIS

One of the most significant uncertainty factors in TOPSIS model is the land developer's opinion on the weighting factor between the environment and the economy, which is assumed to be 0.33 Env. :0.66 Econ. in our model.

To test and analyze the sensitivity of the model proposed, the weighting factor is changed from  $(0.2 : 0.8) \sim (0.8 : 0.2)$ , increasing by increments of (+0.1 : -0.1).

However, although the judging indexes changed, the overall ranking never changed drastically. Most notably, the first two choices stayed the same throughout, as can be seen in Figure 11. This demonstrates the reliability and stability of TOPSIS and, thus, the reliability and stability of its suggestion of the "best" land development option.



Figure 11 TOPSIS Result Fluctuation Under Distinct Weighting

# 5 Task 3: Re-evaluation for Micron Tech., Inc.

In October 2022, it was announced that Micron Technology, Inc. will build a large semiconductor fabrication facility (fab) in Clay, a town just north of Syracuse. The fab is projected to bring with it many more jobs, and thus many more people. To account for the changes that this fab brings to the local community, we re-evaluate affected criteria and re-run our model based off of this.

# 5.1 Affected Factors

The question announces the establishment of a new large semiconductor fabricator(fab) near the land being modelled, which is expected to have a significant impact on local employment, production value, and tourism attraction. To comprehensively assess the impact of the new fab on our metrics, one needs to carefully consider these factors' influence on the data and model.



Figure 12 Affected Factors



#### 5.1.1 Change in Facility Profit

- **Solar array:** Solar array heavily relies on the requirement of energy in the local community. The introduction of the fab will increase the demand for energy, thereby increasing the profit of solar arrays.
- **Crop farms; agrivoltaic farms; regenerative farms; and ranch:** As food quality plays a decisive factor in Americans' selection for food, the newly built fab will significantly decrease the profit of these facilities as the demand for the product reduces.
- **Sports Complex, Cross-country ski/trail:** Both of these facilities' profit relies heavily on attraction and the living conditions of their local community. As this fad is estimated to introduce 49,000 more jobs with a high annual salary of over \$100,000, a significant rise in profit can be predicted.
- **Agritourist center:** Agritourist center's resultant influence is a double-edged sword. The introduction of fab boosts its tourism attraction while decreasing the demand for its agricultural goods.

**Table 11** Estimated Adjustment to the Facility Profit, Contrast in Figure 13

Measurement	Sports Comp.	Ski/Trail	Crop F.	Ranch	Regen. F.	Sol. Arr.	Agritrst Cn.	Agrvltc F.
$P_j$ (\$ $acre^{-1}$ )	13557.69 ↑	382.43↑	161.35↓	509.26↓	287.37↓	21070.95↑	3999.91 -	193.58↓

#### 5.1.2 Change in Restrictions

Many restrictions in the linear programming systems are based on the land's property. With the introduction of the fab, some of these factors need to be reconsidered.

- Employment Index Restriction Removed: As this new fab introduces 9000 direct jobs with 100,000 annual salaries and more than 40,000 indirect jobs, the restriction for the employment index  $\sum_{i=1}^{n} O_i \times x_i^A \ge 4500$  can be removed.
- Tourism Attraction Index Restriction Reduced: This fab greatly increases tourism and resident attraction, so the attraction index limit is reduced to 1000. ∑<sub>i=1</sub><sup>n</sup> A<sub>i</sub> × x<sub>i</sub><sup>A</sup> ≥ 1000

# 5.2 New Plan

Using the same linear programming and TOPSIS with minor changes to the models discussed above, one could determine the ideal environmental, economical, and overall.

Facilities	Sports Comp.	Ski/Trail	Crop F.	Ranch	Regen. F.	Sol. Arr.	Agritrst Cn.	Agrvltc F.
Environment Ideal (acres)	0	0	0	0	0	510-	147—	84-
Economic Ideal (acres)	123↓	0	0	128↑	0↓	$487\uparrow$	3↑	0
Overall Ideal (acres)	123↓	0	0	128↑	0↓	$487\uparrow$	3↑	0

Table 12	Proposed Plan in the Presence of the Fa	ab
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#### Economic Ideal and Overall Ideal:

• Annual profit: \$12006300↑

- **Environment Ideal:** 
  - Annual profit: \$11350400-
- Annual Carbon Emission: −1533120kg↓
- Annual Carbon Emission: -1869100kg-

With the given TOPSIS statistics, Genetic Algorithm can calculate the optimal placements of the facilities as is shown in Figure 14. For specific data, see Appendix B Table 21)



Figure 14 Distribution of Facilities With Fab

In conclusion, with the introduction of the new fab that brings forward many opportunities and change, the annual profit will see a significant rise of over 30% and the annual carbon emission of over 45%. However, alongside these benefits is a decrease in the environmental degradation index of 11%.

# 6 Task 4: Generalizability

The most distinct aspect of this piece of land lies in the fact that the land is in a rural environment. This means that there are far fewer restrictions around the use of the land, which allows purely mathematical

modelling to approach an answer that is far more applicable in real life. Thus, in considering the generalizability of this model, one must also keep in mind that this model will be the most realistically applicable in rural environments due to its very nature.

### 6.1 Familiar Contexts

(Note: The land in New York will be called "original"; our familiar land will be called "new".) Some of our team members have ancestry in Shenzhen, China, so Shenzhen will be used as the familiar context in discussing this model's applicability. The new land can be seen below, under Figure 15. It is 3km<sup>2</sup> in size and lies roughly 26km east of the city center. Many new considerations exist for this plot, as can be seen in Table 13.



Factor	Change(s)
Pop. Density	Adjust restrictions for $P$ , $O_i$ , $A_i$
Climate	Remove cross-country skiing option
Landscape	Adjustments to genetic algorithm and land distribution
Urbanization	Restrictions around development size and emissions

Figure 15New Land in Shenzhen

- **Population Density:** The population of Shenzhen is far greater than that of Syracuse, with 12.59 million for the former and 0.15 million for the latter [12]. As was the case in Task 3, more people means that developments that attract people will increase in profit, and developments that don't will decrease. Restrictions around *P*, *O<sub>i</sub>*, and *A<sub>i</sub>* should be adjusted accordingly.
- **Climate:** The climate in Shenzhen is subtropical, whereas the climate around Syracuse is continental [12]. This has implications for any building types that include outdoor requirements. Additionally, a subtropical climate makes it impossible for cross-country skiing to be viable at all.
- Landscape: The original plot was only somewhat close to certain freshwater lakes and had five different land types: forest, crop, wetland, developed and shrub. The new plot, however, is very close to the South China Sea, and has three land types: forest, wetland, and developed. The genetic algorithm must be modified to consider only these three land types, and changes must be made to accommodate the new percentage distribution of each.
- Urbanization: Since the new land is so close to the Shenzhen city center, it will be heavily influenced by urban planning. New restrictions should be placed around the maximum size of a given development, and social factors  $R_i$  and  $S_i$  should be adjusted to reflect the different needs and wants of an urban society. Restrictions around carbon emissions E should also be tighter, to reflect the increased seriousness of pollution in cities.

### 6.2 Land in Other Countries

When considerations are expanded to an international level, many of the same parallels remain. As long as considerations and adjustments are made to reflect the characteristics of the plot of land (such as urban/rural setting, climate, landscape, and unique factors), our model can be applied and will be able to present a solution. This reflects the versatility of linear programming: as long as variables are related in a linear fashion, the model will produce results.

# 7 Conclusion and Evaluation

# 7.1 Evaluation of Strengths and Weaknesses

#### Strengths

- Linear programming allows maximizing of the land's potential within given constraints, ensuring that the output is as ideal as possible. The simplex algorithm is also highly efficient, drastically reducing the time needed to calculate.
- TOPSIS provides a straightforward method for finding an optimal solution when distinct or even conflicting criteria are present and require a desired weighting factor.
- Genetic algorithm is powerful due to its ability to perform a global search, even in complex and nonlinear search spaces. It also tends to converge to a good solution thanks to the diversity maintained within the population.

#### Weaknesses

- Linear programming is limited to problems with linear and continuous relationships between decision variables and the objective function. Additionally, it is highly sensitive to input data, so small differences in data can result in significant changes in output.
- While TOPSIS assumes normalized data without outliers, outliers can still affect rankings and lead to incorrect conclusions. Furthermore, because it requires the selection of a weighting factor, TOPSIS results introduce subjectivity, making them less reliable objectively.
- Genetic algorithms can be time-consuming, requiring a large number of function evaluations to find a good solution, leading to severe time complexity. Additionally, they can get stuck in local optima, where the algorithm finds a suboptimal solution that is better than its neighbours but not the global optimum.

### 7.2 Conclusion

The objective of this paper is to develop a comprehensive, quantitative approach for determining the optimal planning and allocation of land. Our team achieves this by proposing a base mathematical model that integrates linear programming, TOPSIS, and genetic algorithm. This model considers seven factors that belong to either economic or social benefits, or environmental detriments. Furthermore, a short and long-term analysis model incorporating key factors like inflation, labour cost, and operating cost is included to evaluate the time-based feasibility of plans proposed by the base model. Results show that the model is successful in determining the most optimal planning and allocation of land, even in unfamiliar situations, such as new fabrication facilities built nearby or densely populated urban areas. A sensitivity analysis also reveals the stability of TOPSIS results and possible approaches to further enhance each criteria in linear programming. These findings demonstrate the versatility and applicability of the proposed approach in a variety of contexts, as well as its reliability in producing results.

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nates

	Wetland	Developed	Forest	Crop
Biodiversity	8	1	9	2
Soil Erosion	7	0	10	2
Pollution	9	0	8	1
Total	24	1	27	5
<i>E</i> Factor	6	29	3	25

#### Table 14 Environmental Degradation Penalties

# Table 15DevelopedCoordinates

lower-left vertex	higher-right vertex
(3.5, 1.5)	(5, 4)
(11.5, 0.5)	(12.5, 2)
(0, 14)	(0.5, 15)
(5.5, 13.5)	(7, 15)
(19, 7)	(20, 11)
(16, 15)	(17, 16.5)

lower-left vertex	higher-right vertex
(0, 3.5)	(3.5, 10)
(5, 0)	(9, 4)
(4.5, 7)	(6, 8.5)
(7.5, 7)	(11, 10.5)
(4, 12.5)	(5, 15)
(14.5, 0)	(19, 5)
(17.5, 8)	(19, 10)

Table 16 Crop Land Coordi-

#### Table 17Wetland Coordinates

lower-left vertex	higher-right vertex
(3.5, 4)	(5, 6.5)
(8, 12)	(11.5, 18.5)

# Appendix B All learning Curves and Final DNA of Genetic Algorithm

			1	
Occupation rate	Fitness	Best DNA string	Learning Curve	Converted DNA string in the form of [x, y, width]
0.4	1620.1	0 1 0 0 1 0 0 0 0 0 1 0 1 0 1 0 1 1 0 0 1 0 1	1600 1550 1450 1450 1450 1450 1450 1450 14	Sports Comp. [5.8, 7.3, 5.2] Regen. F. [0.0, 9.0, 3.2] Sol. Arr. [6.5, 0.0, 12.9] Agritrst Cn. [16.1, 7.3, 3.2]
0.5	1899.7	0 1 1 0 1 0 0 0 0 1 0 1 0 1 1 0 0 1 0 1	1900 1850 1800 1750 1700 1650 0 50 100 150 200 250 300 350 403	Sports Comp. [7.7, 7.9, 5.2] Regen. F. [0.0, 11.9, 7.7] Sol. Arr. [6.5, 0.0, 12.9] Agritrst Cn. [19.1, 8.5, 0.6]
0.6	2020.2	0 1 1 0 1 0 0 0 0 1 0 1 0 1 1 0 1 1 0 1 1 0 0 1 0 0 0 0	2025 2000 1975 1990 1925 1900 1875 1850 0 59 100 150 200 250 390 350 400	Sports Comp.[8.4, 6.8, 5.8] Regen. F. [0.0, 9.0, 5.2] Sol. Arr. [6.5, 0.0, 12.9] Agritrst Cn. [17.4, 8.5, 1.9]

 Table 18
 Further DNA-related Data of the TOPSIS Overall Best option with 0.4 - 0.6 Occupation Rate

Occupation rate	Fitness	Best DNA string	Learning Curve	Converted DNA string in the form of [x, y, width]
0.4	1246.9	$\begin{array}{c} 0 \ 1 \ 1 \ 1 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 1 \ 0 \ 1 \ 1 \ 0 \\ 1 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 0 \$		Sol. Arr.[0.0, 9.0, 12.9] Agritrst Cn. [14.2, 0.0, 4.5] Agrvltc F. [6.5, 0.0, 5.8]
0.5	1473.2	01111010 00000011 00000010 10010010 000000	$ \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \end{array}\\ \end{array}\\ \begin{array}{c} \end{array}\\ \begin{array}{c} \end{array}\\ \begin{array}{c} \end{array}\\ \end{array}\\ \begin{array}{c} \end{array}\\ \begin{array}{c} \end{array}\\ \begin{array}{c} \end{array}\\ \begin{array}{c} \end{array}\\ \end{array}\\ \begin{array}{c} \end{array}\\ \begin{array}{c} \end{array}\\ \begin{array}{c} \end{array}\\ \begin{array}{c} \end{array}\\ \end{array}$	Sol. Arr. [5.2, 2.3, 14.2] Agritrst Cn. [0.6, 9.0, 19.4] Agrvltc F. [10.3, 0.0, 9.7]
0.6	1455.7	0 1 0 1 0 0 1 0 0 0 0 0 1 1 0 1 0 0 1 1 1 1	1455	Sol. Arr. [5.2, 2.3, 14.8] Agritrst Cn. [3.9, 10.7, 7.7] Agrvltc F. [12.3, 11.9, 4.5]

**Table 19**Further DNA-related Data of the Economic best option with 0.4 - 0.6 Occupation Rate

Occupation rate	Fitness	Best DNA string	Learning Curve	Converted DNA string in the form of [x, y, width]
0.4	1530.6	0 0 1 0 0 0 0 0 0 0 1 0 1 0 1 0 0 1 1 0 1 0		Sport Comp. [2.6, 6.2, 10.3] Ranch [0.0, 13.0, 10.3] Sol. Arr. [6.5, 0.0, 12.3] Agritrst Cn. [8.4, 10.2, 1.3]
0.5	1761.1	0 0 1 0 0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 0	1760 1750 1740 1740 1740 1740 1700 1900 0 50 100 150 200 250 300 350 400	Sports Comp. [2.6, 5.6, 10.3] Ranch [0.0, 12.4, 11.0] Sol. Arr. [6.5, 0.0, 12.3] Agritrst Cn. [0.0, 14.7, 1.3]
0.6	1996.2	$\begin{array}{c} 1 \ 0 \ 1 \ 1 \ 0 \ 0 \ 1 \\ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \\ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 0 \$	2000 1950 1960 1860 1860 1750 1650 0 59 100 150 200 250 300 350 400	Sports Comp. [14.2, 0.0, 5.8] Ranch [5.8, 0.6, 7.1] Sol. Arr.[0.6, 7.9, 11.0] Agritrst Cn. [3.9, 7.3, 1.9]

**Table 20**Further DNA-related Data of the Environmental best option with 0.4 - 0.6 Occupation Rate

Occupation rate & Cases	Fitness	Best DNA string	Learning Curve	Converted DNA string in the form of [x, y, width]
Environmen tal 0.5	1374.6	0 1 1 0 0 0 0 0 1 0 0 1 0 0 1 1 0 0 0 0	1350 1300 1250 1200 1150 0 50 100 150 200 250 300 350 400	Sol. Arr. [0.6, 7.9, 13.5] Agritrst Cn. [2.6, 5.1, 10.3] Agrvltc F.[15.5, 0.0, 3.2]
Economic / All 0.5	1684.1	0 0 0 1 0 0 0 0 0 0 1 0 1 0 0 1 0 0 0 1 0 1	1675 1690 1625 1600 1575 1550 1550 0 50 100 150 200 250 300 350 400	Sports Comp. [1.3, 12.4, 10.3] Ranch [0.0, 9.0, 20.0] Sol. Arr. [6.5, 0.0, 12.3] Agritrst Cn. [5.2, 11.9, 9.7]

**Table 21**Further DNA-related Data of different best option with 0.5 Occupation Rate with the addition offactory

# Appendix C Genetic Algorithm Code

GA Process	Code Lines
Objective Function Conversion Natural Selection Reproduction	[84~224] [230~244] [247~254] [257~262]
Mutation	[265~269]

Table 22Appendix Code of GA Processes

.....

..... import numpy as np import matplotlib.pyplot as plt  $DNA\_SIZE = 5 * 3 * 4$ # DNA length POP\_SIZE = 1000 # population size # mating probability (DNA crossover)  $CROSS_RATE = 0.8$ MUTATION\_RATE = 0.002 # mutation probability  $N_GENERATIONS = 400$  $length_bound = [1, 20]$ # x upper and lower bounds  $x_{bound} = [0, 20]$  $y_{bound} = [0, 17.5]$ # Python program to find total area of two # overlapping Rectangles # Returns Total Area of two overlap # rectangles def binary\_to\_decimal(binary\_string): decimal = 0for i in range(len(binary\_string)): digit = int(binary\_string[i]) power = 4 - i

Visualize Genetic Algorithm to find a maximum point in a function.

```
decimal += digit * (2 ** power)
return decimal

def overlappingArea(l1, r1, l2, r2):
    x = 0
    y = 1
    ''' Length of intersecting part i.e
    start from max(l1[x], l2[x]) of
    x-coordinate and end at min(r1[x],
```

 $x_{dist} = (\min(r1[x], r2[x]) -$ 

 $y_dist = (min(r1[y], r2[y]) -$ 

max(l1[x], l2[x]))

max(l1[y], l2[y]))

lengths '''

r2[x]) x-coordinate by subtracting
start from end we get required

```
areaI = 0
   if x_dist > 0 and y_dist > 0:
       areaI = x_dist * y_dist
   return areaI
#all environmental factors
Ew = 30 - 24
Ed = 30 - 1
Ef = 30 - 27
Ec = 30 - 5
osc_area = 267 * 0.6 / 2.709
rf_area = 129 * 0.6 / 2.709
sa_area = 344 * 0.6 / 2.709
ac_area = 1 * 0.6 / 2.709
cro = [[[4, 12.5], [5, 15]],
      [[17.5, 8], [19, 10]],
      [[7.5, 7], [11, 10.5]],
      [[4.5, 7], [6, 8.5]],
      [[0, 3.5], [3.5, 10]],
      [[14.5, 0], [19, 5]],
      [[5, 0], [9, 4]]]
dev = [[[16, 15], [17, 16.5]],
       [[0, 14], [0.5, 15]],
       [[5.5, 13.5], [7,15]],
       [[19, 7], [20, 11]],
       [[3.5, 1.5], [5, 4]],
       [[11.5, 0.5], [12.5, 2]]]
wet = [[[8, 12], [11.5, 18.5]],
         [[3.5, 4], [5, 6.5]]]
squareconstrains = [[[0, 15], [8, 17.5]],
                 [[0, 17.5], [20, 1000]],
                 [[20, 0], [1000, 17.5]]]
def F(osc_x, rf_x, sa_x, ac_x, osc_y, rf_y, sa_y, ac_y, osc_width, rf_width, sa_width, ac_width):
   global osc_area, rf_area, sa_area, ac_area, dev, cro, wet, Ew, Ec, Ef, Ed
   total = 0
   if(osc_width == 0):
       return 0
   if (rf_width == 0):
       return 0
   if (sa_width == 0):
       return 0
   if (ac_width == 0):
      return 0
   osc_length = osc_area / osc_width
   rf_length = rf_area / rf_width
   sa_length = sa_area / sa_width
   ac_length = ac_area / ac_width
   if(osc_y < -8.5/6 * osc_x + 8.5):
       return 0
   if (rf_y < -8.5 / 6 * rf_x + 8.5):
```

```
return 0
if (ac_y < -8.5 / 6 * ac_x + 8.5):
   return 0
if (sa_y < -8.5 / 6 * sa_x + 8.5):</pre>
   return 0
if (osc_y + osc_length > -7.5 / 4.5 * (osc_x + osc_width) + 44.33333):
   return 0
if (rf_y + rf_length > -7.5 / 4.5 * (rf_x + rf_width) + 44.33333):
   return 0
if (ac_y + ac_length > -7.5 / 4.5 * (ac_x + ac_width) + 44.33333):
   return 0
if (sa_y + sa_length > -7.5 / 4.5 * (sa_x + sa_width) + 44.33333):
   return 0
osc = [[osc_x, osc_y], [osc_x + osc_width, osc_y + osc_length]]
rf = [[rf_x, rf_y], [rf_x + rf_width, rf_y + rf_length]]
sa = [[sa_x, sa_y], [sa_x + sa_width, sa_y + sa_length]]
ac = [[ac_x, ac_y], [ac_x + ac_width, ac_y + ac_length]]
#Outdoor Sport Complex
area = osc_area
#developed
for i in range(0, 6):
   total += Ed * overlappingArea(osc[0], osc[1], dev[i][0], dev[i][1])
   area -= overlappingArea(osc[0], osc[1], dev[i][0], dev[i][1])
   area -= overlappingArea(osc[0], osc[1], dev[i][0], dev[i][1])
#Crop
for i in range(0, 7):
   total += Ed * overlappingArea(osc[0], osc[1], cro[i][0], cro[i][1])
   area -= overlappingArea(osc[0], osc[1], cro[i][0], cro[i][1])
#Wetland
for i in range(0, 2):
   total += Ed * overlappingArea(osc[0], osc[1], wet[i][0], wet[i][1])
   area -= overlappingArea(osc[0], osc[1], wet[i][0], wet[i][1])
#taking off the part that is not in the map
for j in range(0, 3):
   if (overlappingArea(osc[0], osc[1], squareconstrains[j][0], squareconstrains[j][1]) > 0):
       return 0
total += area * Ef
# Regenetive farm
area = rf_area
# developed
for i in range(0, 6):
   total += Ed * overlappingArea(rf[0], rf[1], dev[i][0], dev[i][1])
   area -= overlappingArea(rf[0], rf[1], dev[i][0], dev[i][1])
# Crop
for i in range(0, 7):
   total += Ec * overlappingArea(rf[0], rf[1], cro[i][0], cro[i][1])
   area -= overlappingArea(rf[0], rf[1], cro[i][0], cro[i][1])
# Wetland
for i in range(0, 2):
   total += Ew * overlappingArea(rf[0], rf[1], wet[i][0], wet[i][1])
   area -= overlappingArea(rf[0], rf[1], wet[i][0], wet[i][1])
```

```
# taking off the part that is not in the map
for j in range((0, 3)):
   if (overlappingArea(rf[0], rf[1], squareconstrains[j][0], squareconstrains[j][1]) > 0):
      return 0
total += area * Ef
#Solar array
area = sa_area
# developed
for i in range(0, 6):
   total += Ed * overlappingArea(sa[0], sa[1], dev[i][0], dev[i][1])
   area -= overlappingArea(sa[0], sa[1], dev[i][0], dev[i][1])
# Crop
for i in range(0, 7):
   total += Ec * overlappingArea(sa[0], sa[1], cro[i][0], cro[i][1])
   area -= overlappingArea(sa[0], sa[1], cro[i][0], cro[i][1])
# Wetland
for i in range(0, 2):
   total += Ew * overlappingArea(sa[0], sa[1], wet[i][0], wet[i][1])
   area -= overlappingArea(sa[0], sa[1], wet[i][0], wet[i][1])
# taking off the part that is not in the map
for j in range(0, 3):
   if (overlappingArea(sa[0], sa[1], squareconstrains[j][0], squareconstrains[j][1]) > 0):
      return 0
total += area * Ef
# agriculture center
area = ac_area
# developed
for i in range(0, 6):
   total += Ed * overlappingArea(ac[0], ac[1], dev[i][0], dev[i][1])
   area -= overlappingArea(ac[0], ac[1], dev[i][0], dev[i][1])
# Crop
for i in range(0, 7):
   total += Ec * overlappingArea(ac[0], ac[1], cro[i][0], cro[i][1])
   area -= overlappingArea(ac[0], ac[1], cro[i][0], cro[i][1])
# Wetland
for i in range(0, 2):
   total += Ew * overlappingArea(ac[0], ac[1], wet[i][0], wet[i][1])
   area -= overlappingArea(ac[0], ac[1], wet[i][0], wet[i][1])
# taking off the part that is not in the map
for j in range(0, 3):
   if (overlappingArea(ac[0], ac[1], squareconstrains[j][0], squareconstrains[j][1]) > 0):
      return 0
total += area * Ef
#check if 4 rectangles touch each other
if(overlappingArea(ac[0], ac[1], sa[0], sa[1]) > 0):
   return 0
if (overlappingArea(osc[0], osc[1], sa[0], sa[1]) > 0):
   return 0
if (overlappingArea(rf[0], rf[1], sa[0], sa[1]) > 0):
   return 0
```

```
if (overlappingArea(rf[0], rf[1], ac[0], ac[1]) > 0):
       return 0
   if (overlappingArea(rf[0], rf[1], osc[0], osc[1]) > 0):
       return 0
   if (overlappingArea(osc[0], osc[1], ac[0], ac[1]) > 0):
      return 0
   return total
# find non-zero fitness for selection
def get_fitness(pred): return pred
# convert binary DNA to decimal and normalize it to a range(0, 5)
def translateDNA(pop):
   newpop = []
   for i in range(0, POP_SIZE):
      newpop.append([])
   for i in range(0, POP_SIZE):
       for j in range(0, DNA_SIZE//3, 5):
          string = str(pop[i][j]) + str(pop[i][j+1]) + str(pop[i][j+2]) + str(pop[i][j+3]) +
              str(pop[i][j+4])
          newpop[i].append(binary_to_decimal(string) / float(2**5-1) * x_bound[1])
       for j in range(DNA_SIZE//3, DNA_SIZE//3 * 2, 5):
          string = str(pop[i][j]) + str(pop[i][j+1]) + str(pop[i][j+2]) + str(pop[i][j+3]) +
              str(pop[i][j+4])
          newpop[i].append(binary_to_decimal(string) / float(2**5-1) * y_bound[1])
       for j in range(DNA_SIZE//3 * 2, DNA_SIZE, 5):
          string = str(pop[i][j]) + str(pop[i][j+1]) + str(pop[i][j+2]) + str(pop[i][j+3]) +
              str(pop[i][j+4])
          newpop[i].append(binary_to_decimal(string) / float(2**5-1) * length_bound[1])
   return newpop
def select(pop, fitness): # nature selection wrt pop's fitness
   if(fitness.sum() == 0):
      pop = np.random.randint(2, size=(POP_SIZE, DNA_SIZE))
      return pop
   else:
       idx = np.random.choice(np.arange(POP_SIZE), size=POP_SIZE, replace=True,
                       p=fitness/(fitness.sum()))
   return pop[idx]
def crossover(parent, pop): # mating process (genes crossover)
   if np.random.rand() < CROSS_RATE:</pre>
       i_ = np.random.randint(0, POP_SIZE, size=1)
                                                                      # select another individual
          from pop
       cross_points = np.random.randint(0, 2, size=DNA_SIZE).astype(bool) # choose crossover points
       parent[cross_points] = pop[i_, cross_points]
                                                                      # mating and produce one child
   return parent
def mutate(child):
   for point in range(DNA_SIZE):
       if np.random.rand() < MUTATION_RATE:</pre>
          child[point] = 1 if child[point] == 0 else 0
```

```
return child
```

```
pop = np.random.randint(2, size=(POP_SIZE, DNA_SIZE)) # initialize the pop DNA
new_row = np.array([1,0, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0,
   0, 0, 0, 1, 0, 1 ,1, 1, 1, 0, 1,1, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 1, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0,
   0, 1])
pop[0] = new_row
a = []
b = []
for _ in range(N_GENERATIONS):
   a.append(_)
   print("This is generation ->", _)
   F_values = []
   list2 = translateDNA(pop)
   for i in range(0, POP_SIZE):
      list1 = list2[i]
      F_values.append(F(list1[0], list1[1], list1[2], list1[3],
               list1[4], list1[5], list1[6], list1[7],
               list1[8], list1[9], list1[10], list1[11])) # compute function value by extracting
                  DNA
   F_values = np.asarray(F_values)
   print(F_values, "F_values")
   fitness = get_fitness(F_values)
   b.append(max(fitness))
   print(max(fitness))
   print("Most fitted DNA: ", pop[np.argmax(fitness), :])
   pop = select(pop, fitness)
   pop_copy = pop.copy()
   for parent in pop:
       child = crossover(parent, pop_copy)
       child = mutate(child)
                          # parent is replaced by its child
      parent[:] = child
```

```
plt.scatter(a, b)
plt.show()
```

# Appendix D Genetic Algorithm DNA Graph Code

```
sa_area = 344 * 0.6 / 2.709
ac_area = 1 * 0.6 / 2.709
DNA\_SIZE = 5 * 3 * 4
                            # DNA length
POP_SIZE = 400 # population size
CROSS_RATE = 0.8
                     # mating probability (DNA crossover)
MUTATION_RATE = 0.003 # mutation probability
N_GENERATIONS = 1000
length_bound = [1, 20]
                         # x upper and lower bounds
x_{bound} = [0, 20]
y_{bound} = [0, 17.5]
area = [osc_area, rf_area, sa_area, ac_area]
def drawrec(l1, l2, r1, r2):
   pen.penup()
   pen.goto(11, 12)
   pen.pendown()
   pen.goto(l1, r2)
   pen.goto(r1, r2)
   pen.goto(r1, 12)
   pen.goto(11, 12)
newstring = ""
for x in range(0, 119, 2):
   newstring += string[x]
def binary_to_decimal(binary_string):
   decimal = 0
   for i in range(len(binary_string)):
       digit = int(binary_string[i])
       power = 4 - i
       decimal += digit * (2 ** power)
   return decimal
def translateDNA(given):
   newpop = [[],[],[],[]]
   for j in range(0, DNA_SIZE//3, 5):
       string = str(given[j]) + str(given[j + 1]) + str(given[j + 2]) + str(given[j+3]) +
          str(given[j+4])
      newpop[(j) // 5].append(binary_to_decimal(string) / float(2**5-1) * x_bound[1])
   for j in range(DNA_SIZE//3, DNA_SIZE//3 * 2, 5):
       string = str(given[j]) + str(given[j+1]) + str(given[j+2]) + str(given[j+3]) +
          str(given[j+4])
      newpop[(j-20) // 5].append(binary_to_decimal(string) / float(2**5-1) * y_bound[1])
   for j in range(DNA_SIZE//3 * 2, DNA_SIZE, 5):
       string = str(given[j]) + str(given[j+1]) + str(given[j+2]) + str(given[j+3]) +
          str(given[j+4])
      newpop[(j-40) // 5].append(binary_to_decimal(string) / float(2**5-1) * length_bound[1])
   return newpop
array = translateDNA(newstring)
print(array)
x =10
pen.goto(6 * x, 0)
pen.goto(0, 8 * x)
pen.goto(0, 15 * x)
pen.goto(8 * x, 15 * x)
pen.goto(8 * x, 17.5 * x)
pen.goto(15.5 * x, 17.5 * x)
```

# Appendix E Linear Programming Code

```
% Create optimization variables
b = optimvar("b",1,8,"LowerBound",0);
% Set initial starting point for the solver
initialPoint.b = zeros(size(b));
% Create problem
problem = optimproblem("ObjectiveSense", "Maximize");
% Define problem objective
problem.Objective = 0.05 * (-4.86) * (200 * b(1) +50*b(2)
   -25*b(3)+500*b(4)-20*b(5)-3330*b(6)-2*b(7)-2030*b(8)) + 0.95 * 2 * (13557.69* b(1))
   +382.43*b(2) + 161.35*b(3) + 509.26*b(4) + 287.37*b(5) +
   21070.95*b(6)+3999.91*b(7)+193.58*b(8));
% Define problem constraints
problem.Constraints.constraint1 = sum(b) <= 741;</pre>
problem.Constraints.constraint2 = 3 * b(1) +4*b(2) +8*b(3)+9*b(4)+9*b(5)+3*b(6)+6*b(7)+7*b(8) >=
   3000:
problem.Constraints.constraint3 = 10 * b(1) +9*b(2) +b(3)+2*b(4)+2*b(5)+b(6)+9*b(7)+2*b(8) >=
   2000;
problem.Constraints.constraint4 = 9.5* b(1) +b(2) +7.5 * b(3)+ 8.5*b(4)+8.5*b(5)+2.5 *
   b(6)+9*b(7)+7.5*b(8) >= 4500;
problem.Constraints.constraint5 = 9.5* b(1) +8 * b(2) +b(3)+ b(4)+1.5*b(5)+ b(6)+7*b(7)+b(8) >=
   1500;
% Display problem information
```

show(problem);

% Solve problem
[solution,objectiveValue,reasonSolverStopped] = solve(problem,initialPoint);

% Display results solution

reasonSolverStopped

objectiveValue

% Remove Variable

clearvars b initialPoint reasonSolverStopped objectiveValue

# Appendix F TOPSIS Code

```
#include<iostream>
#include<cmath>
using namespace std;
int main(){
     double pr;
     double eco;
     double array1[8];
     double bd, wd;
     double array[8][8] = {
    \{123, 0, 0, 128, 0, 487, 3, 0\},\
    \{0, 0, 0, 0, 0, 510, 147, 84\},\
    \{0, 0, 0, 0, 54, 536, 151, 0\},\
    \{0, 0, 0, 0, 2, 511, 147, 81\},\
    \{0, 0, 0, 0, 0, 510, 147, 84\}
    };
     for(int i = 0; i < 5;i ++){</pre>
           pr = 13557.69 * array[i][0] + 382.43 * array[i][1] + 161.35 * array[i][2]
               + 509.26 * array[i][3] + 287.37 * array[i][4] + 21070.95 * array[i][5]
               + 3999.91 * array[i][6] + 193.58 * array[i][7];
           eco = 200 * array[i][0] + 50 * array[i][1] - 25 * array[i][2]
                + 500* array[i][3] - 20 * array[i][4] - 3330 * array[i][5] - 2 * array[i][6]
                - 2030 * array[i][7];
           cout<<pre>cout<<endl<<eco<<endl;</pre>
           bd = sqrt(pow(2 * (12006000 - pr),2) + pow(4.86 * (-1869100 - pr),2));
           wd = sqrt(pow(2 * (118250 - pr),2) + pow(4.86 * (351000 - pr),2));
           array1[i] = wd/(bd + wd);
     }
     for (int i = 0; i < 5; i + +){
           cout<<array1[i]<<endl;</pre>
     }
     return 0;
}
```